



## THE BOUNDARY VALUE PROBLEM FOR EQUATION OF A MOBILE SECOND KIND TYPE WITH OFFSET

**Abraev B.X.**

The Termiz state of university.

**Gulmirzayeva S.M**

Termiz state of university.

**Tilavov I.A.**

The Termiz state of university.

### ABSTRACT

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**KEY WORDS:** Equation, curved, field, sphere, half-plane, characterize, the affixes, parabolic, degeneration, intersect, stick.

1. The setting task. Consider the equation

$$U_{xx} + \text{sign}y|y|^m U_{yy} + \alpha|y|^{m-1}U_y = 0 \quad (0 < m < 2) \quad (1)$$

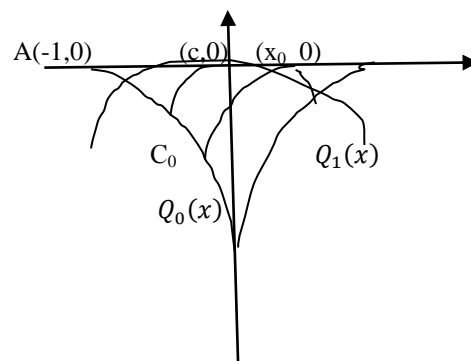
Where,  $(\alpha = \text{const}) \quad m - 1 < \alpha < 1$  – constantly in a simple connected D bounded by a smooth curve G with ends at the points A(-1,0) and B(1,0) located in the half-plane  $y > 0$  and characteristics.

AC:  $x - \frac{2}{2-m}(-y)^{\frac{2-m}{2}} = -1$     BC:  $x + \frac{2}{2-m}(-y)^{\frac{2-m}{2}} = 1$     equation (1). We introduce following notations:

$$Q_0(x) = \frac{x_0 - 1}{2} - i \left[ \frac{2-m}{4} (x_0 + 1) \right]^{\frac{2}{2-m}}$$

B(1,0)

$$Q_1(x) = \frac{x_0 + 1}{2} - i \left[ \frac{2-m}{4} (1 - x_0) \right]^{\frac{2}{2-m}}$$



where  $Q_0(x)$  и  $Q_1(x)$  are the affixes on the points of interection of the characteristics of equation (1), from the points  $x_0 \in (-1; 1)$ , with the characteristics of AC and BC respectively.

**Task.** Finding the function of  $U(x, y)$ , having next to characters:

- 1).  $U(x; y) \in C(\bar{D})$
- 2).  $U(x; y)$  – constant solution of the equation (1) at field  $D^+$
- 3).  $U(x; y)$  – generalize solution of the equation (1) of class of  $R_2$  at field  $D^-$
- 4). On line  $y=0$  parabolic degeneration of the equations (1) are doing conditions sticks

$$U(x, +0) = U(x, -0) , \quad -1 \leq x \leq 1$$

$$v(x) = \lim_{y \rightarrow -0} (-y)^\alpha \frac{\partial U}{\partial y} = - \lim_{y \rightarrow +0} y^\alpha \frac{\partial U}{\partial y} \quad -1 \leq x \leq 1 \quad (2)$$

5)  $U(x; y)$  satisfies boundary conditions.  $U|_\Gamma = \varphi(s) \quad s \in \Gamma$   $u|_{AC_0} =$   
 $\psi(x) \quad (3)$

$$U[Q_0(x)] + \mu U[Q_1(x)] = \rho(x) \quad (-1 \leq x \leq 1) \quad (4)$$

where  $\mu = const \neq 0$ ,  $\rho(x)$  - continuous has piecewise continuous first order derivatue on the segment  $[-1,1]$ . [1]

2. Functional relationship between  $T(x)$  and  $v(x)$  .

In the half-plane  $y < 0$  the equation accepts view.

$$U_{xx} - (-y)^m U_{yy} + \alpha (-y)^{m-1} U_y = 0$$

It can find by means of characteristic coordinates

$$\xi = x - \frac{2}{2-m} (-y)^{\frac{2-m}{2}} , \quad \eta = x + \frac{2}{2-m} (-y)^{\frac{2-m}{2}} \quad \text{it is converted to the Eyley-Darbu equation:}$$

$$\frac{\partial^2 u}{\partial \xi \partial \eta} - \frac{\beta}{\eta - \xi} \left( \frac{\partial u}{\partial \eta} - \frac{\partial u}{\partial \xi} \right) = 0 \quad [1] \quad (5)$$

$$\text{where } \beta = \frac{2\alpha - m}{2(2-m)} , \quad \frac{1}{2} < \beta < 0 \quad \text{so } m - 1 < \alpha < \frac{m}{2} \quad (6)$$

It is known that generalize solution  $U(x; y) \in R_2$  equations (5) satisfying the initial date. ([1])

$$U(x; 0) = \tau(x)$$

$$v(x) = \lim_{y \rightarrow -0} (-y)^\alpha \frac{\partial u}{\partial y} = \left( \frac{2-m}{2} \right)^{2\beta} \lim_{\eta - \xi \rightarrow 0} (\eta - \xi)^{2\beta} \left( \frac{\partial u}{\partial \xi} - \frac{\partial u}{\partial \eta} \right) \quad -1 < x < 1$$

$$\text{has the from } U(\xi, \eta) = \int_{-1}^{\xi} (\eta - t)^{-\beta} (t - \xi)^{-\beta} T(t) dt + \frac{1}{2\cos\pi\beta} \int_{\xi}^{\eta} (\eta - t)^{-\beta} (t - \xi)^{-\beta} T(t) dt - \chi_2 \int_{\xi}^{\eta} (\eta - t)^{-\beta} (t - \xi)^{-\beta} v(t) dt \quad (7)$$

$$\text{where } \chi_2 = \frac{\Gamma(2-2\beta)}{(1-\alpha)\Gamma^2(1-\beta)} \left( \frac{2-m}{4} \right)^{1-2\beta} \quad (8)$$

$$\tau(x) = \tau(-1) + \int_{-1}^x (x-t)^{-2\beta} T(t) dt \quad (9)$$

Without loss of generality, we assume  $\tau(-1) = 0$

From solution (7) we have

$$u[Q_1(x)] = \int_{-1}^c (x-t)^{-\beta} (c-t)^{-\beta} T(t) dt + \frac{1}{2\cos\pi\beta} \int_{-1}^x (x-t)^{-\beta} (t+1)^{-\beta} T(t) dt - \chi_2 \int_{-1}^x (x-t)^{-\beta} (t+1)^{-\beta} v(t) dt =$$

$$\Gamma(1-\beta) D_{-1,c}^{\beta-1} (c-x)^{-\beta} T(x) + \frac{\Gamma(1-\beta)}{2\cos\pi\beta} D_{c,x}^{\beta-1} (x-c)^{-\beta} T(x) - \chi_2 \Gamma(1-\beta) D_{c,x}^{\beta-1} (x-c)^{-\beta} v(x)$$

at  $c = -1$ ,  $Q_1(x) = Q_0(x)$  as well as

$$u[Q_0(x)] = \frac{\Gamma(1-\beta)}{2\cos\pi\beta} D_{-1,x}^{\beta-1} (x+1)^{-\beta} T(x) - \chi_2 \Gamma(1-\beta) D_{-1,x}^{\beta-1} (x+1)^{-\beta} v(x)$$

On the boundary condition (4) we use operator  $D_{c,x}^{1-\beta}$  and obtain.

$$D_{c,x}^{1-\beta} u[Q_0(x)] + \mu D_{c,x}^{1-\beta} u[Q_1(x)] + D_{c,x}^{1-\beta} \rho(x)$$

$$D_{c,x}^{1-\beta} u[Q_0(x)] = \frac{d}{dx} \left[ \frac{1}{\Gamma(\beta)} \int_c^x \frac{u[Q_0(t)]}{(x-t)^{1-\beta}} dt + \frac{1}{\Gamma(\beta)} \int_{-1}^c \frac{u[Q_0(t)]}{(x-t)^{1-\beta}} dt - \frac{1}{\Gamma(\beta)} \int_{-1}^c \frac{u[Q_0(t)]}{(x-t)^{1-\beta}} dt \right]$$

$$= D_{-1,x}^{1-\beta} u[Q_0(x)] - \frac{d}{dx} \frac{1}{\Gamma(\beta)} \int_{-1}^c \frac{u[Q_0(t)]}{(x-t)^{1-\beta}} dt$$

Use of equality from this

$$D_{-1,x}^{1-\beta} u[Q_0(x)] = \mu D_{c,x}^{1-\beta} u[Q_1(x)] + \rho_1(x) \tag{10}$$

where  $\rho_1(x) = D_{c,x}^{1-\beta} \rho(x) + \frac{d}{dx} \frac{1}{\Gamma(\beta)} \int_{-1}^c \frac{u[Q_0(t)]}{(x-t)^{1-\beta}} dt$  [2]

Now, we count

$$D_{c,x}^{1-\beta} u[Q_1(x)] = D_{c,x}^{1-\beta} \left\{ \Gamma(1-\beta) D_{-1,c}^{\beta-1} (c-x)^{-\beta} T(x) + \frac{\Gamma(1-\beta)}{2\cos\pi\beta} D_{c,x}^{\beta-1} (x-c)^{-\beta} T(x) - \chi_2 \Gamma(1-\beta) D_{c,x}^{\beta-1} (x-c)^{-\beta} v(x) \right\}$$

$$= \Gamma(1-\beta) D_{c,x}^{1-\beta} D_{-1,c}^{\beta-1} (c-x)^{-\beta} T(x) + \frac{\Gamma(1-\beta)}{2\cos\pi\beta} (x-c)^{-\beta} T(x) - \chi_2 \Gamma(1-\beta) (x-c)^{-\beta} v(x)$$

These equality boundary condition (10)

$$D_{-1,x}^{1-\beta} \left\{ \frac{\Gamma(1-\beta)}{2\cos\pi\beta} D_{-1,c}^{\beta-1} (x+1)^{-\beta} T(x) - \chi_2 \Gamma(1-\beta) D_{-1,c}^{\beta-1} (x+1)^{-\beta} v(x) \right\} = \frac{\Gamma(1-\beta)}{2\cos\pi\beta} (x+1)^{-\beta} T(x) - \chi_2 \Gamma(1-\beta) (x+1)^{-\beta} v(x)$$

From here

$$\frac{\Gamma(1-\beta)}{2\cos\pi\beta} (x+1)^{-\beta} T(x) - \chi_2 \Gamma(1-\beta) (x+1)^{-\beta} v(x) = \mu \Gamma(1-\beta) D_{c,x}^{1-\beta} D_{-1,c}^{\beta-1} (c-x)^{-\beta} T(x) + \mu \frac{\Gamma(1-\beta)}{2\cos\pi\beta} (x-c)^{-\beta} T(x) - \chi_2 \mu \Gamma(1-\beta) (x-c)^{-\beta} v(x) + \rho_1(x)$$

We carry out don't be complex transformations and will find

$$v(x) = \frac{T(x)}{2\chi_2 \cos\pi\beta} - \mu \theta(x) + \rho_2(x) \tag{11}$$

Where  $\omega(x) = \frac{(x+1)^{-\beta} - \mu(x-c)^{-\beta}}{(x+1)^\beta (x-c)^\beta}$ ,  $\theta(x) = \frac{\mu}{\omega(x)} D_{c,x}^{1-\beta} (c-x)^{-\beta} D_{-1,c}^{\beta-1} T(x)$

$$\rho_2(x) = \frac{\rho_1(x)}{\omega(x) \Gamma(1-\beta)}$$

Formula (11) gives the first functional relation between  $T(x)$  and  $v(x)$ , which is determined from the condition that the  $U(x; y)$  of equation (1) of the domen  $D^-$  must satisfy the boundary condition (4).

**THE LIST OF LITERATURE**

- 1). Смирнов М.М. Уравнения смешанного типа. М.: Наука 1970, 242с.
- 2). Мирсабуров М. Сингуляр коэффициентли геллерстедт тенгламаси учун трикоми масаласи. Ўқув қўлланма 2007 й.