



MASS TRANSFER COEFFICIENTS IN AN ABSORBER RECTOR IN THE UNIT OPERATIONS LABORATORY, THE TEMPERATURE PROFILE (2)

Mariano Pérez Camacho¹

¹Departamento de Ingeniería Química,
UNAM, Facultad de Estudios Superiores
Zaragoza,
Ciudad de México C.P. 09230

Antonio Valiente Barderas²

²Departamento de Ingeniería Química,
UNAM, Facultad de Química,
Ciudad de México C.P. 04510

Ricardo Pérez Camacho³

³Departamento de Ingeniería Química,
UNAM, Facultad de Química,
Ciudad de México C.P. 04510

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ABSTRACT

In the first article Mass Transfer Coefficients in an Absorber Reactor in the Unit Operations Laboratory (1) reference [4], it was developed by students of the Faculty of Chemistry of the National Autonomous University of Mexico, UNAM. Students now obtain the temperature profile along the column by posing and solving the differential equation of energy balance (heat) that is a function of the temperatures of the liquid with the position $TL = TL(z)$ and compare the results with experimental values that were obtained with thermocouples distributed every 22 cm throughout the top of the column. To solve the energy equation numerically, it is necessary to use the matter balance program developed in reference [4], to calculate the value of the individual coefficient of mass transfer on the liquid side k_L and with this value obtain the absorption speed in the presence of a chemical reaction at the interface using successive iterations of calculation and thus numerically solving the temperature profile of the liquid vs. the position in the column. With this type of experimentation, the teaching by competences is reinforced, a necessary teaching that a chemical engineer must possess.

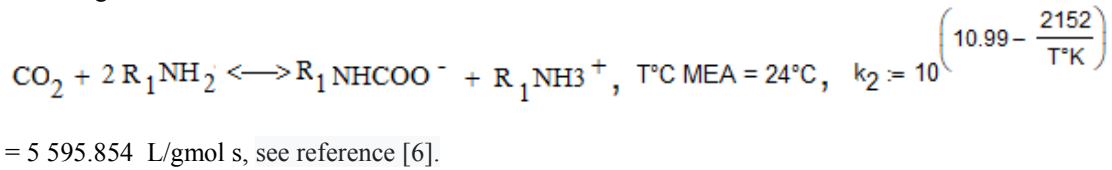
KEYWORDS: Balances of matter and energy in absorption with chemical reaction. MEA-H₂O / CO₂-air reaction system. Thermodynamic balance between phases in the presence of chemical reaction. Teaching by competencies.

1. INTRODUCTION

Chemical engineering education today is based on so-called competencies. Professional competencies are those that are learned during the career and that include the specific knowledge of the same, as well as the professional skills and attitudes of the students. The UNAM Chemical Engineering Laboratory is one of the places where these skills can be developed and refined through the development of laboratory experimentations, since during these apprenticeships' students must use their knowledge and apply it, as well as develop your personal skills and attitudes. In this laboratory unit operations are studied among other disciplines. There chemical engineering students experiment in various equipment, one of which is the absorption tower. In it, students are asked to experimentally find the individual gas-transfer and liquid-side mass transfer coefficients in the presence of a chemical reaction and to compare the temperature profiles of the theoretical models and experimental temperature data throughout the column.

2.- THEORETICAL FOUNDATIONS

It was mentioned in the first article [4] the system (MEA-H₂O / CO₂-AIR) that has a reaction mechanism made up of consecutive reversible reactions, but when adding and canceling the partial terms they generate the following 2nd order reaction and exothermic.



To study now the proposed model of heat as a function of liquid temperatures and the position TL = TL (z) within the column, the students of the Faculty of Chemistry used an absorption tower located in the Chemical Engineering Laboratory of the Faculty of Chemistry of the National Autonomous University of Mexico, UNAM. To do this, it was necessary to vary the experimental operating conditions to make observations and consider possible theoretical and practical simplifications.

For example:

- The reaction is fast enough to develop in the film of the liquid. This study is contemplated in the first article [4].
- The reaction is exothermic and increases the internal temperature in the column with increasing liquid phase feed flow.

2.1 To propose the models of the balance of matter [4] and now that of energy (heat), use Fig. (1)

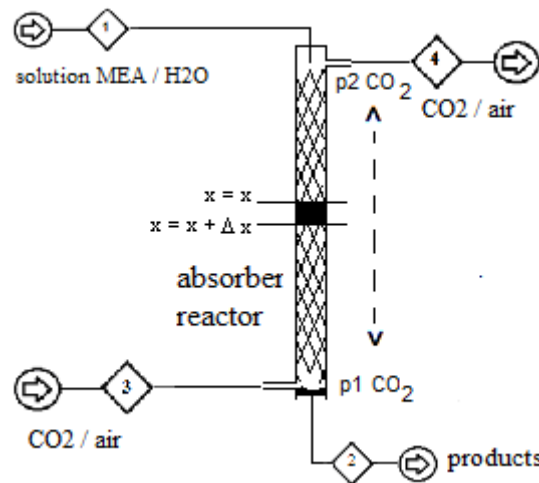


Fig. (1) Absorber Reactor

Assumptions:

- When using high mass flows of MEA / H₂O, the reaction behaves like a pseudo-primer order with respect to solute A (CO₂), [4].
- The longitudinal speed of the liquid is constant, there is no radial or angular speed, [4].
- Radial mixing is perfect, there are no radial concentration gradients.
- Axial diffusion is negligible, compared to convective axial effects.
- The density of the system is practically constant.
- The molar volumetric concentration of the soluble gas in the liquid in the column = 0, all CO₂ reacts in the liquid film.
- The partial pressures along the column have values very close to the values of equilibrium pressures at the interface.
- There are no radial or angular molar fluxes in the absorber-reactor, only longitudinal and temporary.
- Control of mass transfer resides in the film of the liquid phase.

COMMENTARY. - The changes in the z positions along the absorber-reactor of Fig. (1) are obtained by the following differential equation by solving for the z position, for this the partial pressures at the inlet and outlet of the column of known height h.

$$\frac{d^2 p_{CO_2}}{dz^2} = 0$$

border conditions (1)

$$\left. \begin{aligned} p_{CO_2} &= p_{1CO_2} \text{ to } z = 0 \\ p_{CO_2} &= p_{2CO_2} \text{ to } z = h \end{aligned} \right\} \text{solution} \rightarrow p_{CO_2} = \left(\frac{p_{2CO_2} - p_{1CO_2}}{h} \right) z + p_{1CO_2}$$

2.2- The following differential mass balance can be proposed for CO₂ in the liquid phase in the absorber reactor [4]:

$$\begin{aligned} -D_L \varepsilon A_T \frac{\partial [A_0]}{\partial z} \Big|_z + \varepsilon A_T L [A_0] \Big|_z + R_A a \Delta z A_T &= -D_L \varepsilon A_T \frac{\partial [A_0]}{\partial z} \Big|_{z+\Delta z} + \\ \varepsilon A_T L [A_0] \Big|_{z+\Delta z} + \varepsilon A_T \Delta z \frac{\partial [A_0]}{\partial t} - r \varepsilon A_T \Delta z & \end{aligned} \quad (2)$$

Dividing between the control volume ($\varepsilon A_T \Delta z$) and taking limits equation (4) is obtained

$$\lim_{\Delta z \rightarrow 0} \left\{ D_L \frac{\partial [A_0]}{\partial z} \Big|_{z+\Delta z} - D_L \frac{\partial [A_0]}{\partial z} \Big|_z - \frac{L [A_0] \Big|_{z+\Delta z} - L [A_0] \Big|_z}{\Delta z} \right\} = \frac{\partial [A_0]}{\partial t} - \frac{R_A a}{\varepsilon} - r \quad (3)$$

If there is no accumulation in the permanent regime, and disregarding the convective and diffusive terms of the absorbed CO₂, compared to the reaction in the film, and if also the absorption speed with reaction is appreciably greater than the physical absorption speed, we obtain:

$$\cancel{L \frac{\partial [A_0]}{\partial z}} + \cancel{\frac{\partial [A_0]}{\partial t}} - \frac{R_A a}{\varepsilon} - r = \cancel{D_L \frac{\partial^2 [A_0]}{\partial z^2}} \quad (4)$$

convection accumulation Absorption reaction diffusion
with reaction

$$\boxed{-\frac{R_A a}{\varepsilon} - r = 0} \quad (5)$$

2.3.- The following differential mass balance can also be proposed for the monoethanolamine in the liquid phase in the absorber reactor:

$$\varepsilon A_T L [B_0] \Big|_z = \varepsilon A_T L [B_0] \Big|_{z+\Delta z} - r \varepsilon A_T \Delta z \quad (6)$$

Dividing by the control volume ($\varepsilon A_T \Delta z$) and taking limits to equation (6) is obtained

$$\lim_{\Delta z \rightarrow 0} \left\{ \frac{L [B_0] \Big|_{z+\Delta z} - L [B_0] \Big|_z}{\Delta z} \right\} = r$$

$\Delta z \rightarrow 0$

The differential balance for amine is:

$$\boxed{L \frac{d[B_0]}{dz} = r} \quad (7)$$

By equating (5) and (7) we arrive at

$$-\frac{R_A a}{\varepsilon} = L \frac{d[B_0]}{dz}$$

$$L d[B_0] = -\frac{R_A a}{\varepsilon} dz \quad (8)$$

Integrating equation (8) from the top to the bottom of the column we obtain:

$$\boxed{h = -\frac{L \varepsilon}{a} \int_{B_0 \text{ top}}^{B_0 \text{ bottom}} \frac{d[B_0]}{R_A}} \quad \text{ó} \quad \boxed{h = \frac{L \varepsilon}{a} \int_{B_0 \text{ bottom}}^{B_0 \text{ top}} \frac{d[B_0]}{R_A}} \quad (9)$$

2.4- Energy balance on the volume differential element located in some arbitrary distance z of Fig. (1), See reference [1].

Rapid flow of incoming energy = Rapid flow of exiting energy + Accumulated energy - Generated energy - Exchanged energy

If the total energy flux in z is defined as the sum of the diffusive and convective fluxes

$$e_z = q_z + \rho_L C_{pL} v_z (T_L - T_R) \quad (10)$$

Where is the reference temperature (for example, that of the environment)

$$q_z = \frac{Q_z}{A_T} = -k_{axial} \frac{dT_L}{dz} \quad (11)$$

The heat generated by the reaction is:

$$\Phi_H = r (-\Delta H_r), \text{ where } \Delta H_r \text{ is the enthalpy change due to the reaction and } r \text{ is the reaction speed} = -k_{Am} [Am] [CO_2]$$

An equivalent form of this term is to use the diffusive absorption-reaction flux through the interface, where the speed of reaction in the liquid phase does not occur in the bulk of the liquid but in the interfacial region [5], since It is a fast reaction that depends on the diffusive absorption flux.

$$\Phi_H = R_A a (\Delta H_{abs}) \quad (12)$$

Where the heat of absorption $\Delta H_{abs} = (84.68 - 0.1135 \times T_L + 0.0027 \times T_L^2)$ in [kjoules / gmol] reported by Hanne M. Kvamsdal and Magne Hillestad [2], [3]. TL is the temperature of the liquid in the absorber reactor in [° C] and a is the specific gas-liquid interface area [m²/m³]

The volumetric heat loss to the neighborhoods of the column is calculated as:

$$Q_V = -h_{walls} a (T_L - T_{amb})$$

$$\text{Where } h_{walls} = 1000 \times 4.05 \times 10^{-3} \times \left(\frac{\rho_g V_g}{D_{hyd}} \right)^{0.5} (Cp_g)^{0.33} \text{ in [W/m}^2 \text{ K]} \quad (13)$$

$$\rho_g = [kg / m^3], \quad V_g = [m/s], \quad D_{hyd} = [m], \quad Cp_g = [j/m^3 K]$$

The foundations of this coefficient are found in the work of Hanne M. Kvamsdal and Magne Hillestad [2], [3], TL is the temperature of the liquid in the tower and T_{amb} is the ambient temperature.

Substituting the previous equations in the general energy balance described above, the following is obtained:

$$A_T q_z|_z + A_T \rho_L C_{pL} v_z (T_L - T_R)|_z = A_T q_z|_{z+\Delta z} + A_T \rho_L C_{pL} v_z (T_L - T_R)|_{z+\Delta z}$$

$$+ \Delta z A_T \rho_L C_{pL} \frac{dT_L}{dt} - \Delta z A_T \Phi_H - \Delta z A_T Q_V \quad (14)$$



Dividing equation (14) by the control volume $(A_T \Delta z)$ and taking the limit when $\Delta z \rightarrow 0$, the following differential equation is obtained:

$$-k_{axial} \frac{\partial^2 T}{\partial z^2} + \rho_L C_{pL} v_z \frac{\partial T}{\partial z} + \rho_L C_{pL} \frac{\partial T}{\partial t} - \Phi_H - Q_v = 0$$

diffusion o
convection
accumulation
generation
energy
(15)

conduction

exchange

If in equation (15) the term axial conduction is neglected and if this reactor operates continuously in a stable state, then there is no accumulation of energy, it also operates as non-adiabatic and non-isothermal. The following model is obtained:

$$-k_{axial} \frac{\partial^2 T}{\partial z^2} + \rho_L C_{pL} v_z \frac{\partial T}{\partial z} + \rho_L C_{pL} \frac{\partial T}{\partial t} - \Phi_H - Q_v = 0$$

diffusion o
convection
acumulation
generation
energy

conduction

exchange

$$\boxed{\frac{dT}{dz} = \frac{\Phi_H + Q_v}{V_z \rho_L C_{pL}}}$$

(16)

where $v_z = \frac{\text{volumeric flow}}{\text{cross flow area beetwen packages}}$, ρ_L is the density of the liquid and C_{pL} is the specific heat at constant pressure of the liquid.

3.- EXPERIMENTAL DATA AND CALCULATIONS

The equipment used for experimentation was as follows

The equipment has the following specifications:
 Internal column diameter: 5.08 cm
 Flow cross-sectional area (ATF): 14.66 cm²
 Packed height: 106 cm
 Construction material: Glass
 Packaging: External diameter, internal diameter and length glass Raschig rings 0.703 cm 0.545 cm 0.854 cm
 Chromatograph: Gow-Mac electrical conductivity
 Fraction of hollows $\epsilon = 0.70$
 $a = 0.839 \text{ cm}^2/\text{cm}^3$
 $a_t = 7.169 \text{ cm}^2/\text{cm}^3$
 Six thermocouples installed each through the column 22 cm

Absorption tower brand PIGNAT in the Chemical Engineering Laboratory
Fig. (2) Absorber Reactor

3.1 In experimentation the students obtained the following results shown in the Table (1)

Table (1). Experimental Temperature Data

The experimental values of the temperatures were obtained by means of six thermocouples distributed every 22 cm throughout the column, these are interconnected to a MODEM located in the right corner of the equipment and then to the central computer of the Chemical Engineering Laboratory.

Position z (cm)	Temperatures (°C)		
	5 L / h	8 L / h	10 L /h
0	24.1	24.2	24.2
22	28.1	28.5	29.0
44	31.2	32.0	32.4
66	33.2	33.7	35.2
88	34.4	34.6	38.0
110	34.4	36.4	38.9

Table (1). Experimental Data of Flows and Concentrations

Feeding air temperature = 24 °C. Temperature of the fed CO₂ = 23 °C. Hollow fraction $\varepsilon = 0.70$. Inlet air density = $1.204 \cdot 10^{-3} \text{ g / cm}^3$. Cross flow area between packages = 14.66 cm². Inlet CO₂ density = $1.885 \cdot 10^{-3} \text{ g / cm}^3$ Density of the liquid mixture fed 1.004 g / cm^3

Feed flow (L / h)	Concentration MEA N = gmol / Lsol		Concentration MEA (% in mass) % mass = 6.064 (N) + 0.0231 (g MEA / g solution)		Q _{air} (m ³ / h)	Q CO ₂ (L / h)
	entrance	exit	entrance	exit		
5	2.76 N	1.28 N	16.76 %	7.78 %	2.606	257.127
8		1.35 N		8.20 %		
10		1.70 N		10.33 %		

3.2 Evaluation of the terms of the heat balance of the Eq. (16) using the experimental data in Table (1).

$\frac{\partial T}{\partial z} = \frac{\Phi_H + Q_V}{v_z \rho_L C_{pL}}$	$\frac{^\circ\text{C}}{\text{cm}} = \frac{\frac{\text{cal}}{\text{s} \cdot \text{cm}^3} + \frac{\text{cal}}{\text{s} \cdot \text{cm}^3}}{\frac{\text{cm}}{\text{s}} \cdot \frac{\text{gmol}}{\text{cm}^3} \cdot \frac{\text{cal}}{\text{gmol} \cdot ^\circ\text{C}}}$
<p>The speed of the liquid v_z</p> $V_z := \frac{Le \cdot \frac{1}{3600} \cdot \frac{1000}{1}}{\text{ATF}}$ $\frac{\text{cm}}{\text{s}} = \frac{\frac{\text{L}}{\text{h}} \cdot \frac{1\text{h}}{3600 \cdot \text{s}} \cdot \frac{1000\text{cm}^3}{\text{L}}}{\text{cm}^2}$ $V_z = 0.095 \frac{\text{cm}}{\text{s}}$	
<p>The heat capacity of the constant pressure-fed liquid CPL</p> <p>TLe := 24 °C</p> <p>TLe°K := TLe + 273.15</p> $C_{p\text{H}_2\text{O}} := (92.053 - 3.9953 \cdot 10^{-2} \cdot \text{TLe}^\circ\text{K} - 2.1103 \cdot 10^{-4} \cdot \text{TLe}^\circ\text{K}^2 + 5.3469 \cdot 10^{-7} \cdot \text{TLe}^\circ\text{K}^3) \cdot 0.2369$ $\frac{\text{cal}}{\text{gmol} \cdot ^\circ\text{C}} = \frac{\text{Joule}}{\text{gmol} \cdot ^\circ\text{K}} \cdot \frac{0.23901 \cdot \text{cal}}{1 \cdot \text{Joule}}$ $C_{p\text{H}_2\text{O}} = 17.904 \frac{\text{cal}}{\text{gmol} \cdot ^\circ\text{C}}$	



$$T_{Le} := 24 \text{ } ^\circ\text{C}$$

$$T_{Le}^{\circ\text{K}} := T_{Le} + 273.15$$

$$C_{p_{H_2O}} := \left(92.053 - 3.995310^{-2} \cdot T_{Le}^{\circ\text{K}} - 2.110310^{-4} \cdot T_{Le}^{\circ\text{K}^2} + 5.346910^{-7} \cdot T_{Le}^{\circ\text{K}^3} \right) \cdot 0.2369$$

$$\frac{\text{cal}}{\text{gmd} \cdot ^\circ\text{C}} = \frac{\text{Joule}}{\text{gmd} \cdot ^\circ\text{K}} \cdot \frac{0.23901 \text{ cal}}{1 \cdot \text{Joule}}$$

$$C_{p_{H_2O}} = 17.904 \frac{\text{cal}}{\text{gmd} \cdot ^\circ\text{C}}$$

$$C_{p_{MEA}} := \left(23.11 + 1.2283 T_{Le}^{\circ\text{K}} - 3.121810^{-3} \cdot T_{Le}^{\circ\text{K}^2} + 3.071410^{-6} \cdot T_{Le}^{\circ\text{K}^3} \right) \cdot 0.23901$$

$$C_{p_{MEA}} = 46.138 \frac{\text{cal}}{\text{gmd} \cdot ^\circ\text{C}}$$

$$C_{pL} := \left[C_{p_{MEA}} \cdot x_{\text{MolarMEA}} + C_{p_{H_2O}} \cdot (1 - x_{\text{MolarMEA}}) \right]$$

$$C_{pL} = 19.486 \frac{\text{cal}}{\text{gmd} \cdot ^\circ\text{C}}$$

The density of the fed liquid ρ_L

$$\rho_L := \rho_L \cdot \frac{1}{P_{M_{MEA.H_2O}}}$$

$$\frac{\text{gmd} \cdot \text{mezcla}}{\text{cm}^3} = \frac{\text{g} \cdot \text{mezcla}}{\text{cm}^3} \cdot \frac{\text{gmd} \cdot \text{mezcla}}{\text{g} \cdot \text{mezcla}}$$

$$\rho_L = 0.049 \frac{\text{gmol mezcla}}{\text{cm}^3 \text{ mezcla}}$$

Volumetric heat flow through the walls of the column Q_v

$$Q_v = -h_{\text{walls}} \cdot a \cdot (T_L - T_{\text{Amb}})$$

T_L = Variable temperature along the function column (z)

$T_{\text{Amb}} = 24 \text{ } ^\circ\text{C}$

$$a = 0.839 \frac{\text{cm}^2}{\text{cm}^3}$$

The heat transfer coefficient

$$h_{\text{walls}} = 1000 \times 4.05 \times 10^{-3} \times \left(\frac{\rho_g V_g}{D_{\text{hyd}}} \right)^{0.5} (C_{p_g})^{0.33}$$



The hydraulic diameter of tower	<p>Cross flow area ATF = 14.66cm²</p> $R_{\text{torre}} := \sqrt{\frac{\text{ATF} \cdot \left(\frac{1}{100}\right)^2}{\pi}}$ $D_{\text{hyd}} := 2(R_{\text{torre}})$ $D_{\text{hyd}} = 0.043 \text{ m}$
Density of the gaseous mixture fed to the tower	<p>T°Cco2 = 23 °C T°Cair = 24 °C</p> $\rho_{\text{CO}_2} := -5 \cdot 10^{-6} \cdot T^{\circ}\text{Cco}_2 + 0.002 \quad \frac{\text{g}}{\text{cm}^3}$ $\rho_{\text{AIR}} := -4 \cdot 10^{-6} \cdot T^{\circ}\text{Caire} + 0.0013 \quad \frac{\text{g}}{\text{cm}^3}$ $\rho_g := [\rho_{\text{CO}_2} \cdot y_{\text{MolarCO}_2e} + \rho_{\text{AIR}} \cdot (1 - y_{\text{MolarCO}_2e})] \cdot \left(\frac{100}{1}\right)^3 \cdot \frac{1}{1000}$ $\frac{\text{kg}}{\text{m}^3 \text{mezcla}} = \frac{\text{g}}{\text{cm}^3} \cdot \left(\frac{100\text{cm}}{1\text{m}}\right)^3 \cdot \frac{1\text{kg}}{1000\text{g}}$ $\rho_g = 1.284 \quad \frac{\text{kg} \cdot \text{mixture}}{\text{m}^3 \cdot \text{mixture}}$
Speed of gaseous mixture fed to the tower	<p>Q_{air} := 2.606 $\frac{\text{m}^3}{\text{h}}$ Q_{co2} := 257.127 $\frac{\text{L}}{\text{h}}$ ATF = 14.66 cm²</p> <p>T_{air} := 24 °C T°Cco2 := 23 °C</p> <p>Calculate G = 1.284 $\frac{\text{kgmol} \cdot \text{Mixture}}{\text{h}}$</p> <p>Calculate PM_{Air.CO2} = 30.757 $\frac{\text{kg} \cdot \text{Mixture}}{\text{kgmol} \cdot \text{Mixture}}$</p> <p>Calculate ρ_g = 1.284 $\frac{\text{kg} \cdot \text{Mixture}}{\text{m}^3 \cdot \text{Mixture}}$</p> $V_g := G \cdot \frac{1}{3600} \cdot (PM_{\text{Aire.CO}_2}) \cdot \frac{1}{\rho_g} \cdot \frac{1}{\text{ATF}} \cdot 100^2$ $\frac{\text{m}}{\text{s}} = \frac{\text{kgmol} \cdot \text{mezcla}}{\text{h}} \cdot \frac{1\text{h}}{3600 \cdot \text{s}} \cdot \frac{\text{kg}}{\text{kgmol}} \cdot \frac{\text{m}^3}{\text{kg}} \cdot \frac{1}{\text{cm}^2} \cdot \left(\frac{100\text{cm}}{1\text{m}}\right)^2$ <p>V_g = 0.536 $\frac{\text{m}}{\text{s}}$ In these units it is asked in the correlation</p>

Heating capacity at constant pressure of the inlet gas to the tower

$$T^{\circ}\text{Cair} := 24 \quad ^{\circ}\text{C}$$

$$\text{Calculate } C_{p\text{CO}_2} := 38.387 \frac{\text{joule}}{\text{gmol} \cdot ^{\circ}\text{C}}$$

$$\text{Calculate } C_{p\text{AIR}} := 29.138 \frac{\text{joule}}{\text{gmolAIRE} \cdot ^{\circ}\text{C}}$$

$$C_{p_g} := [C_{p\text{CO}_2} \cdot y_{\text{MolarCO}_2e} + C_{p\text{AIR}} \cdot (1 - y_{\text{MolarCO}_2e})]$$

$$\left(\frac{1}{PM_{\text{Aire.CO}_2}} \cdot \rho_g \cdot 1000 \right) \left(\frac{1}{PM_{\text{Aire.CO}_2}} \cdot \rho_g \cdot 1000 \right)$$

$$\frac{\text{Joules}}{\text{m}^3 \cdot ^{\circ}\text{K}} = \left(\frac{\text{joule}}{\text{gmolCO}_2 \cdot ^{\circ}\text{C}} \cdot \frac{\text{gmolCO}_2}{\text{gmolmezcla}} + \frac{\text{joule}}{\text{gmolAIRE} \cdot ^{\circ}\text{C}} \cdot \frac{\text{gmolAIRE}}{\text{gmolmezcla}} \right) \cdot x$$

$$\left(\frac{\text{gmolmezcla}}{\text{gmezcla}} \cdot \frac{\text{kg} \cdot \text{mezcla}}{\text{m}^3 \cdot \text{mezcla}} \cdot \frac{1000\text{g}}{1\text{kg}} \right)$$

$$C_{p_g} = 1261.403 \frac{\text{Joules}}{\text{m}^3 \cdot ^{\circ}\text{K}} \quad \text{are required in these units, see article from Hanne M. Kvmsdal, page 15}$$

Substituting

$$h_{\text{walls}} := \left[1000 \cdot 4.05 \cdot 10^{-3} \cdot \left(\frac{\rho_g \cdot V_g}{D_{\text{hyd}}} \right)^{0.5} \cdot (C_{p_g})^{0.33} \right] \cdot \frac{1}{(1000)} \cdot 239.006 \cdot \frac{1}{100^2}$$

$$\frac{\text{cal}}{\text{s} \cdot \text{cm}^2 \cdot ^{\circ}\text{C}} = \frac{\text{W}}{\text{m}^2 \cdot ^{\circ}\text{K}} \cdot \frac{1\text{kw}}{1000\text{W}} \cdot \frac{239.006 \cdot \frac{\text{cal}}{\text{s}}}{1\text{kw}} \cdot \left(\frac{1\text{m}}{100\text{cm}} \right)^2$$

$$h_{\text{walls}} = 0.0041 \frac{\text{cal}}{\text{s} \cdot \text{cm}^2 \cdot ^{\circ}\text{C}}$$

$$a = 0.839 \text{ cm}^2/\text{cm}^3$$

Heat generated by the reaction

$$\Phi_H = R_A a (-\Delta H_r) \quad \text{Hanne M. Kvmsdal Correlation, page 15 is used}$$

$$\Delta H_r = \Delta H_{\text{absorption}} \quad \text{Hanne M. Kvmsdal Correlation, page 14 is used}$$

$$\Delta H_{\text{abs}} = (84.68 - 0.1135 \cdot T + 0.0027 \cdot T^2) \cdot 1000 \cdot 0.23901$$

$$\frac{\text{cal}}{\text{gmol}} = \frac{\text{kJ}}{\text{gmol}} \cdot \frac{1000\text{J}}{1\text{kJ}} \cdot \frac{0.23901\text{cal}}{1\text{J}}$$

$$R_A := -1 \cdot 10^{-12} \cdot z^3 + 3 \cdot 10^{-11} \cdot z^2 + 2 \cdot 10^{-8} \cdot z + 1 \cdot 10^{-6} \quad \frac{\text{gmolCO}_2}{\text{s} \cdot \text{cm}^2}$$

Relationship obtained with the Appendix A program

4.- RESULTS

4.1 The theoretical and experimental temperature profiles obtained by students

It was resolved Eq. (16) $\frac{dT}{dz} = \frac{\Phi_H + Q_V}{v_z \rho_L C_{pL}}$ numerically using the "Mathematica-Wolfram Research"

program to find the functionality of the temperatures of the liquid phase within the column Vs. the position z the entire length of the reactor-absorber for each experiment of 5, 8 and 10 L / h of fed MEA / H₂O solution. The program with the theoretical results of the first experimentation is attached in Fig. (3).

$$\Delta H_{abs} = (84.68 - 0.1135 * T[z] + 0.0027 * T[z]^2) * 1000 * 0.23901;$$

$$RA = -1 * 10^{-12} * z^3 + 3 * 10^{-11} * z^2 + 2 * 10^{-8} * z + 1 * 10^{-6};$$

$$a = 0.839;$$

$$h_{wall} = 0.0041;$$

$$T_{amb} = 24;$$

$$Q_v = -h_{wall} * a * (T[z] - T_{amb});$$

$$V_z = 0.095;$$

$$\rho_L = 0.049;$$

$$C_{pL} = 19.486;$$

$$\text{sol} = \text{NDSolve} [\{ T' [z] == (\Delta H_{abs} * RA * a + Q_v) / (V_z * \rho_L * C_{pL}), T[0] == T_{amb} \}, T, \{z, 0, 110\}]$$

$$\text{Plot} [\text{Evaluate} [T[z] /. \text{sol}], \{z, 0, 110\}, \text{AxesLabel} \rightarrow \{ "Z [cm]", "T [°C]" \}]$$

$$\text{TableForm} [\{ \{ "z" \text{ cm}, T \text{ °C} \} \}, \text{TableDepth} \rightarrow 2]$$

$$\text{Table} [\{z, T[z] /. \text{sol}\}, \{z, 0, 110, 10\} // \text{TableForm}$$

$$\{ \{ T \rightarrow \text{InterpolatingFunction} \} \}$$

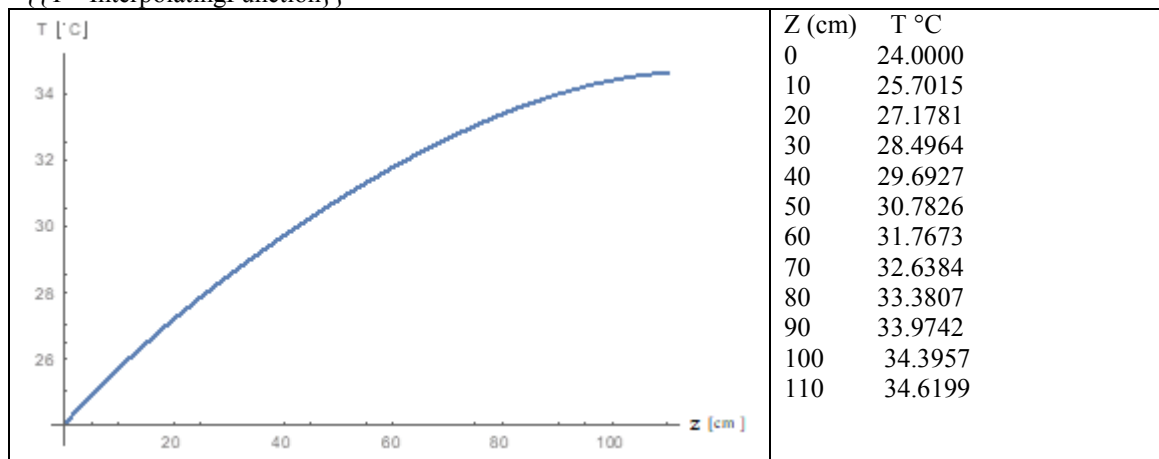
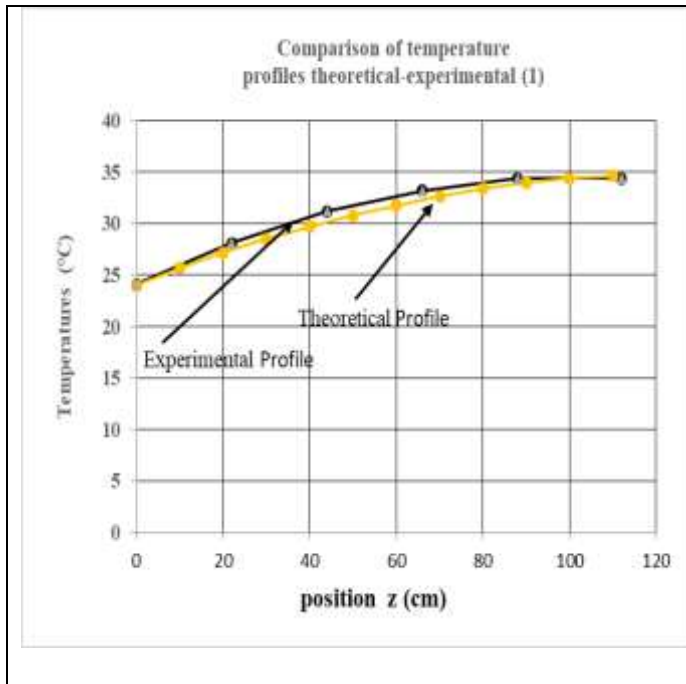
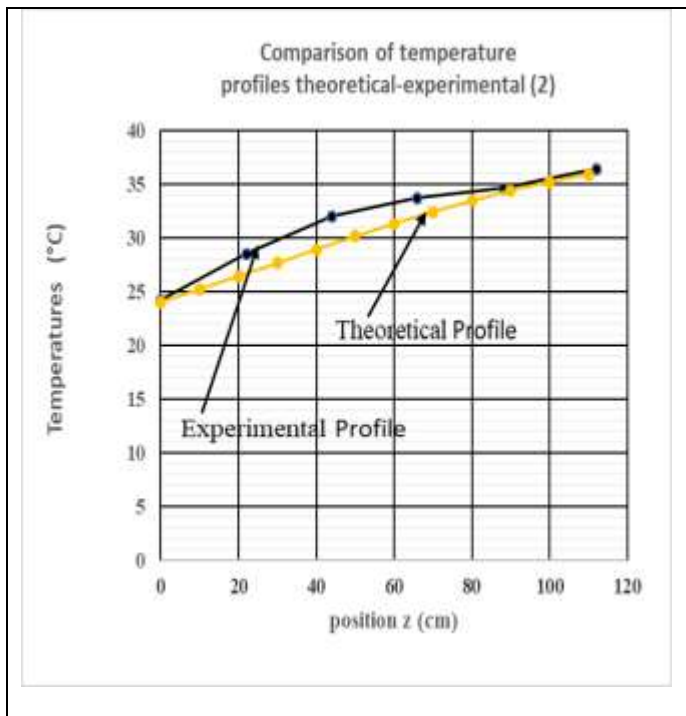


Fig. (3) Theoretical results of the model

In the Fig. (4) the graphical profiles of comparisons of the theoretical and experimental liquid temperatures are shown.



z (cm)	TL (°C)
0	24.1
22	28.1
44	31.2
66	33.2
88	34.4
112	34.4
0	24
10	25.7015
20	27.1781
30	28.4964
40	29.6927
50	30.7826
60	31.7673
70	32.6384
80	33.3807
90	33.9742
100	34
110	34.6199



z (cm)	TL (°C)
0	24.2
22	28.5
44	32
66	33.7
88	34.6
112	36.4
0	24
10	25.1878
20	26.4221
30	27.6743
40	28.92
50	30.1379
60	31.3093
70	32.4174
80	33.447
90	34.3839
100	35
110	35.9247

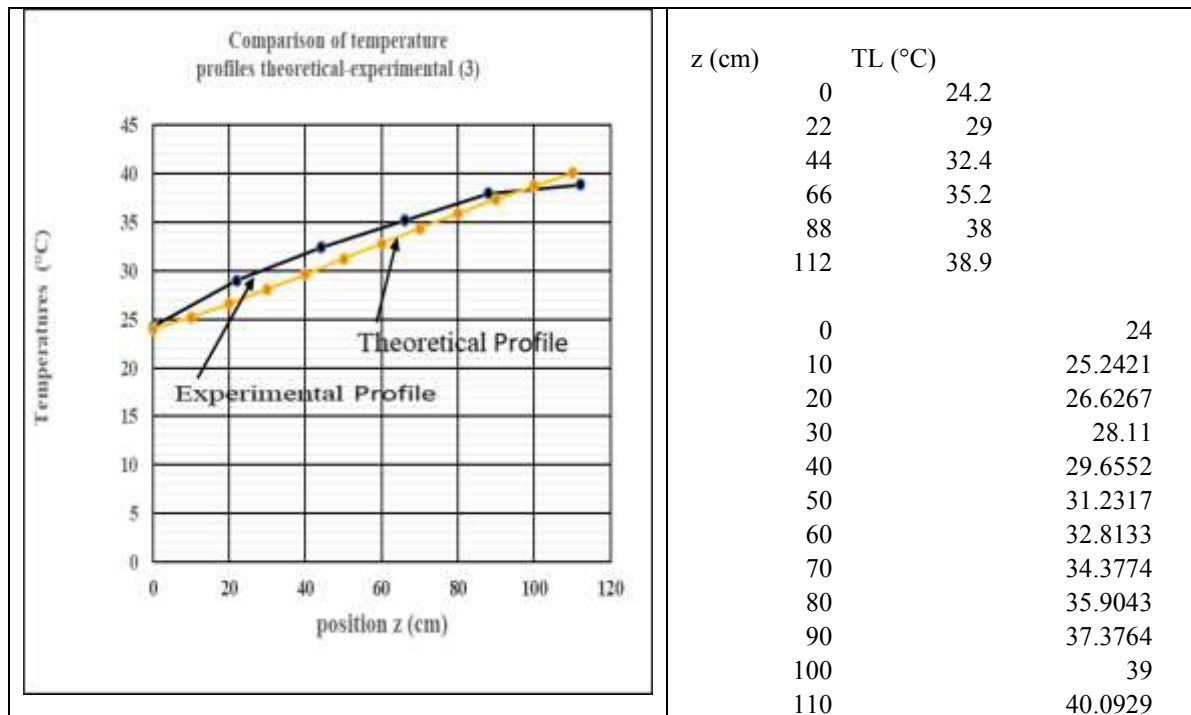


Fig. (4) Comparison of theoretical and experimental curves of liquid temperatures in the column TL (°C) Vs. position z (cm)

5.- CONCLUSIONS

In this experimental study, the students of the Faculty of Chemistry obtained the temperature profiles as shown in Fig. (4), they compare the values in the steady state of temperatures Vs. position of both the model and the values experimental.

It can be seen that increasing the flow of the MEA / H₂O (5, 8, 10) L / h solution increases the temperatures of the phases within the column, this is because initially any element of the interfacial surface is exposed to the penetration of the solute for a time t, but by increasing the flows of liquid fed *Le* residence times decrease $\tau = ATF \times h / Le$ and the surface elements are replaced faster and faster by fresh CO₂ from the gaseous phase, causing an increase in the diffusive flux *R_A* at the interface and that as the amount of CO₂ in the liquid phase increases, the reaction that is exothermic is It will be favored by the limiting reagent transferred, increasing the temperatures inside the column more and more.

6.- NOMENCLATURA

[A₀] = CO₂ concentration in the liquid phase bulk: gmol CO₂ / L solution

a = Effective interfacial area per unit of volume packed: cm²/cm³

a_t = Area of total packing surface per unit volume packed: cm²/cm³

A_T = Cross area of the column: cm²

ATF = Cross-sectional area of flow between packaging: cm²

[A*] = CO₂ interfacial concentration in the film model: gmol CO₂ / L solution

[Bo] = MEA concentration in bulk within the liquid phase: gmol MEA / L solution

BPS = Amina free without reacting at the selected point in the column: gmol MEA / L solution

C* = Concentración del equilibrio termodinámico: gmol MEA / cm³ solution

Cp_g = Specific heat at constant gas pressure: joules/m³ °K; Note. - These are the units required by the correlation (13). [2]

Cp_L = Specific heat at constant pressure from the liquid mixture: cal / gmol mezcla °C

D_L = CO₂ diffusion coefficient in the liquid phase: cm²/s

D_{hyd} = Hydraulic column diameter: cm

E = Enhancement factor

E1 = Enhancement factor formula parameter

Ei = Enhancement factor formula parameter assessed at the interface



GPS = Mass speed at the selected point: gmol mixture /s cm²
 G's = Mass feed air speed: gmol aire /s cm²
 G_{CO2} = Mass feeded CO₂ speed: gmol CO₂ /s cm²
 h = Absorption-reaction column height: cm
h walls = Interfacial heat transfer film coefficient on the walls of the column: watts/m² K
 k_{G a} = Individual and temporal volumetric coefficient on the gas phase side: gmolCO₂ /s cm³ atm
 k_{L a} = Individual and temporal volumetric coefficient on the liquid phase side: 1/ s
Le = Flow of the liquid flow fed: L/ s
 L = Mass liquid speed: cm³ solution/ cm² s
 m = Thermodynamic equilibrium ratio: cm³ atm / gmol CO₂
 Pop = Operating pressure in Mexico City: (0.771) atm
 PM = Molecular mass: g A/gmol A
 p_{CO2} = Partial CO₂ pressure: atm
 p* = Thermodynamic equilibrium pressure: atm
 Q_{CO2} = Carbon dioxide flow: L/h
 Q_{AIR} = Airflow: m³ / h
 Q_V = Volumetric heat to column neighborhoods: cal/ s cm³
 r = Rapid reaction: (cm³/gmol)⁻¹⁺ⁿ /s
 R_A = Rapid absorption with chemical reaction through the interface: gmol A/ s cm²
 t = Operating time: s
Tamb = Environmental temperature: °C
 TL = Temperature of the liquid in the column: °C
 V_g = Speed of the gas mixture in the column: m/s
 V_Z = Speed of liquid mixing in the column: cm/s
 X_{Molar MEA} = Molar fraction of MEA: gmol MEA / gmol mezcla líquida
 W_{MEA} = MEA mass fraction: g MEA /g mezcla
 Z = Arbitrary position in the absorption column: cm
 z = Stoichiometric reaction factor
 ΔH_r = Change of enthalpy due to reaction: cal/gmol
 ΔH_{abs} = Change of enthalpy due to absorption with chemical reaction: cal/gmol
 Φ_H = Volumetric heat generated by the reaction: cal/s cm³
 ε = fraction of gaps between the absorption column packaging
 ρ_G = Density of the gas phase: g/cm³
 ρ_L = Liquid mixture density: gmol/cm³

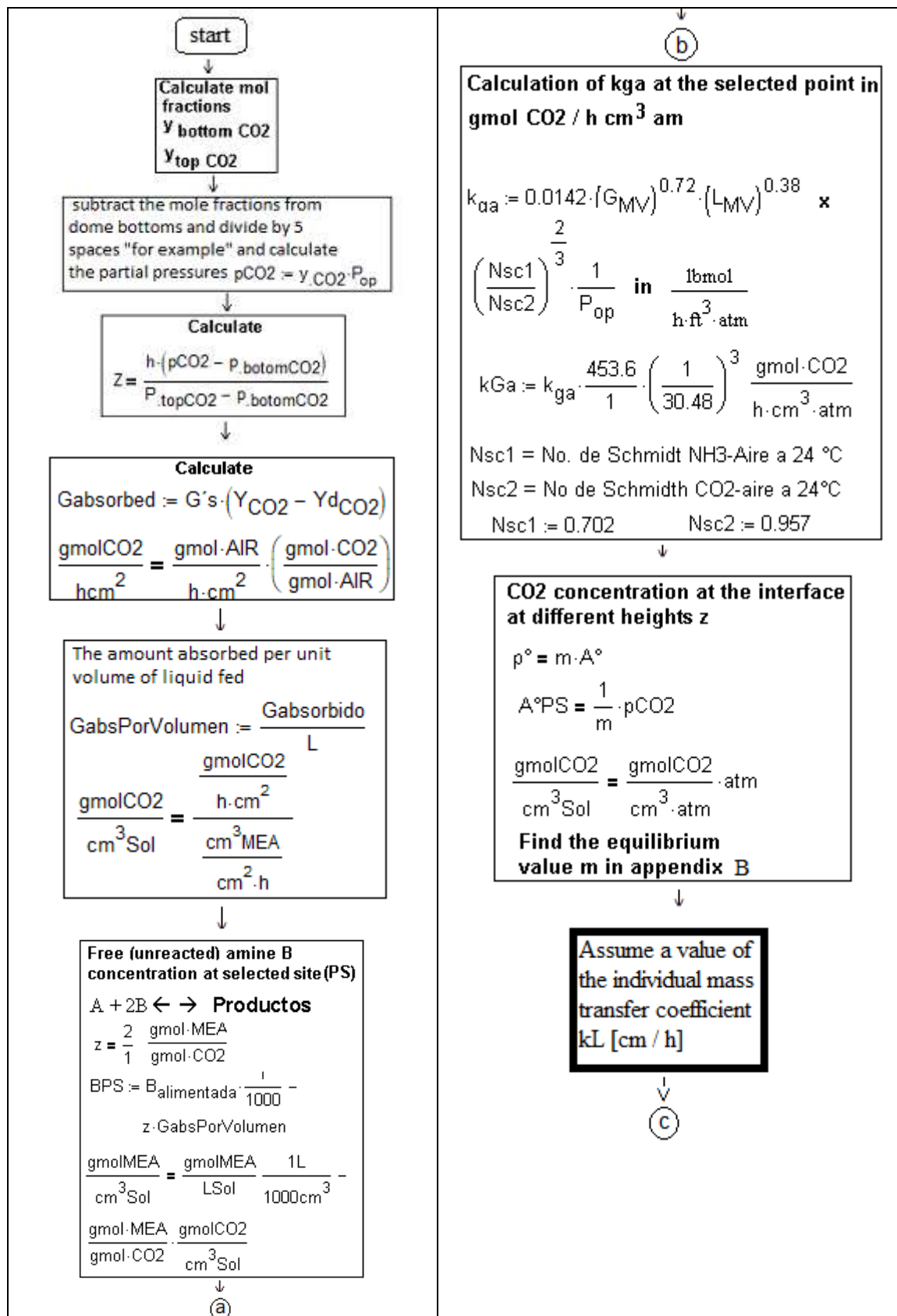
7.- BIBLIOGRAFÍA

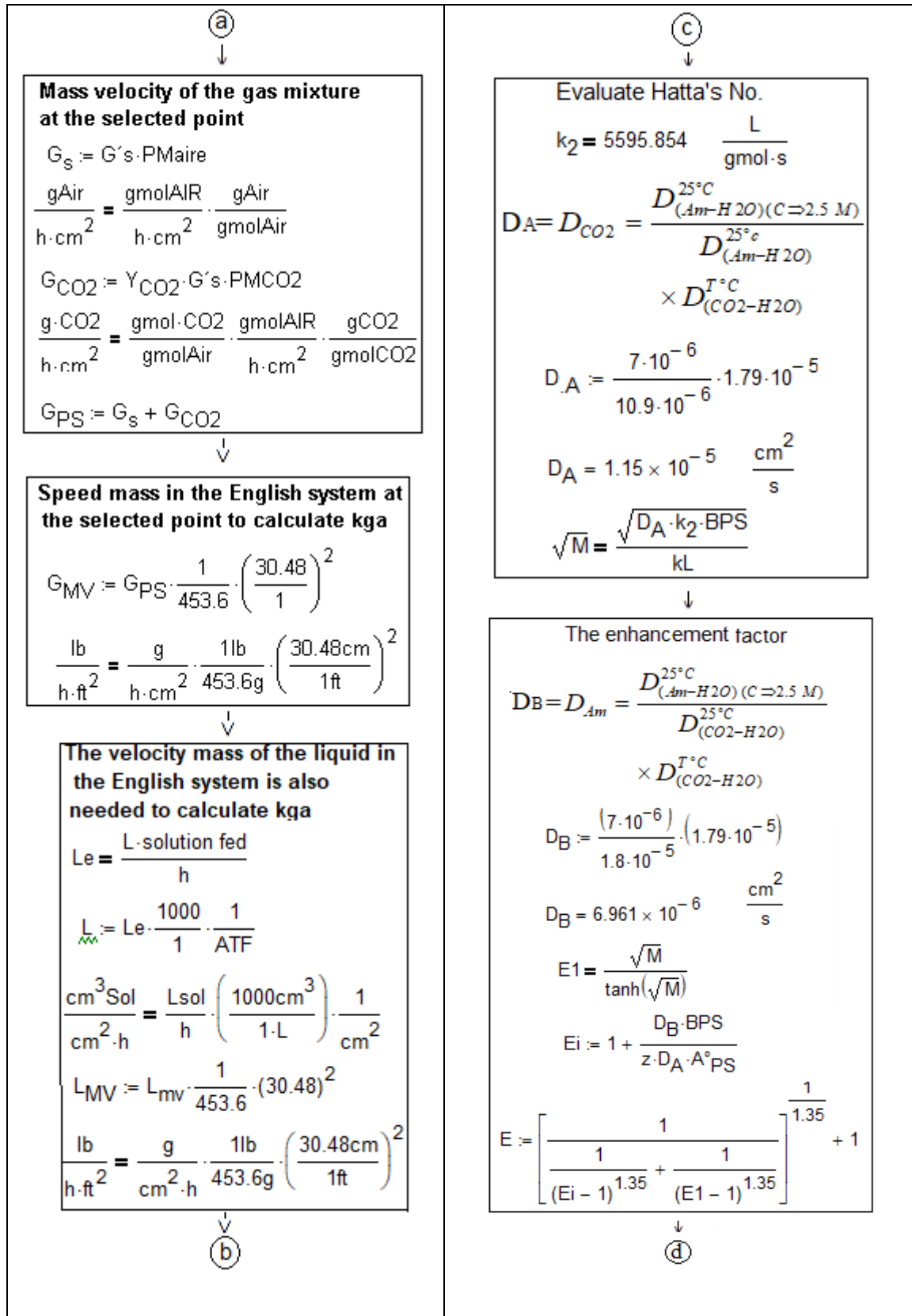
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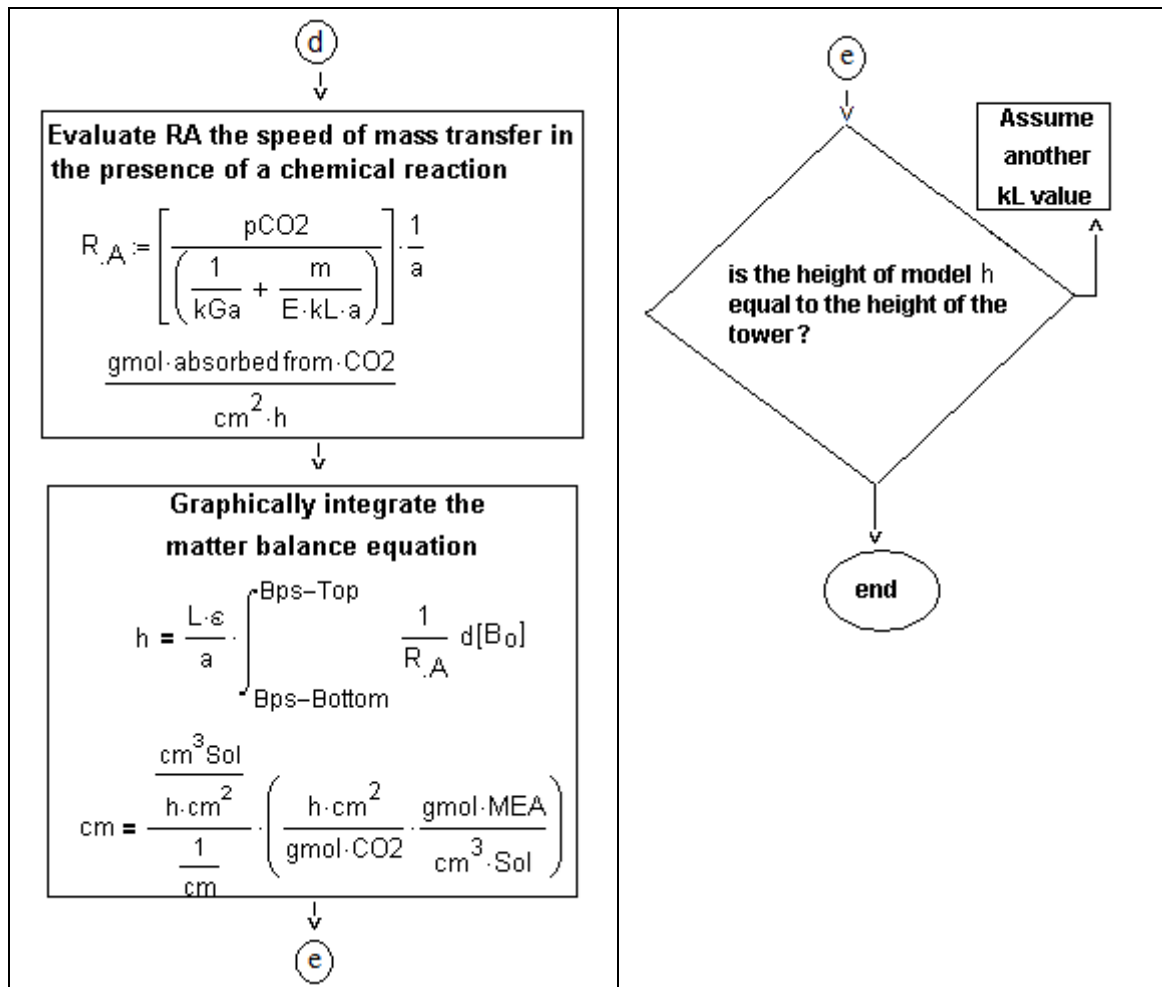
APPENDIX A

To determine quantitatively $\Phi_H = R_A a (\Delta H_{abs})$ it is necessary to calculate the ratio of the diffusive absorption flux with chemical reaction as a function of the z position along the tower and the individual

coefficient of mass transfer on the liquid side k_L . For this, students used the experimental information from Table (1) and the next program used in reference [4].







When the above program equates the height h of the mass balance model with the height of the absorption column, students complete the program and report the values of the individual liquid-side mass transfer coefficient k_L and the fluxes of mass transfer in the presence of chemical reaction at the R_A interface to different positions z along the column.

5 L/h	$z = \begin{pmatrix} 0 \\ 21.16 \\ 42.321 \\ 63.679 \\ 84.84 \\ 106 \end{pmatrix}$ cm	$R_A = \begin{pmatrix} 1.347 \times 10^{-6} \\ 1.744 \times 10^{-6} \\ 2.053 \times 10^{-6} \\ 2.233 \times 10^{-6} \\ 2.203 \times 10^{-6} \\ 1.828 \times 10^{-6} \end{pmatrix}$ gmolCO ₂ / s cm ²
$k_L = 48.7$ cm / h		

$$R_A := -1 \cdot 10^{-12} \cdot z^3 + 3 \cdot 10^{-11} \cdot z^2 + 2 \cdot 10^{-8} \cdot z + 1 \cdot 10^{-6}$$

8 L/h	$z = \begin{pmatrix} 0 \\ 21.16 \\ 42.321 \\ 63.679 \\ 84.84 \\ 106 \end{pmatrix}$	$R_A = \begin{pmatrix} 1.247 \times 10^{-6} \\ 1.769 \times 10^{-6} \\ 2.2 \times 10^{-6} \\ 2.519 \times 10^{-6} \\ 2.714 \times 10^{-6} \\ 2.758 \times 10^{-6} \end{pmatrix}$



$kL = 40.8$ cm / h	cm $gmolCO_2 / s cm^2$ $R_A := -7 \cdot 10^{-14} \cdot z^3 - 1 \cdot 10^{-10} \cdot z^2 + 2 \cdot 10^{-8} \cdot z + 1 \cdot 10^{-6}$
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$10 L/h$	$z = \begin{pmatrix} 0 \\ 21.16 \\ 42.321 \\ 63.679 \\ 84.84 \\ 106 \end{pmatrix}$	$R_A = \begin{pmatrix} 1.069 \times 10^{-6} \\ 1.792 \times 10^{-6} \\ 2.447 \times 10^{-6} \\ 3.022 \times 10^{-6} \\ 3.494 \times 10^{-6} \\ 3.847 \times 10^{-6} \end{pmatrix}$
$kL = 66.8$ cm / h		
	cm $gmolCO_2 / s cm^2$ $R_A := 9 \cdot 10^{-14} \cdot z^3 - 1 \cdot 10^{-10} \cdot z^2 + 2 \cdot 10^{-8} \cdot z + 1 \cdot 10^{-6}$	

APENDICE B

B.1 Thermodynamic equilibrium data for the system (monoethanolamine/water) - (carbon dioxide / air), in the presence of chemical reaction, reports it **Donal L. Katz** [5].

$T = 37.77 \text{ }^\circ\text{C} = 100 \text{ }^\circ\text{F}$					
$X^* = \frac{gmol CO_2}{gmol MEA}$	$p^* = mm Hg$				
0	0	0.53994	34.728	0.64304	276.72
0.05	0	0.56128	56.058	0.64934	294.67
0.10	0	0.57409	70.811	0.65562	317.51
0.15	0	0.58262	85.535	0.66383	379.47
0.20	0	0.58902	103.50	0.66587	397.4
0.25	0	0.59756	126.37	0.67212	425.12
0.30	0	0.60183	142.7	0.67408	457.72
0.35	0	0.61037	162.31	0.68032	488.71
0.4	0	0.61677	180.27	0.68447	509.91
0.43908	0	0.62424	200.05	0.6865	531.1
0.46951	3.2785	0.62843	214.74	0.690	555.56
0.49885	9.9449	0.63261	231.05	0.69687	576.54
		0.63676	253.88		

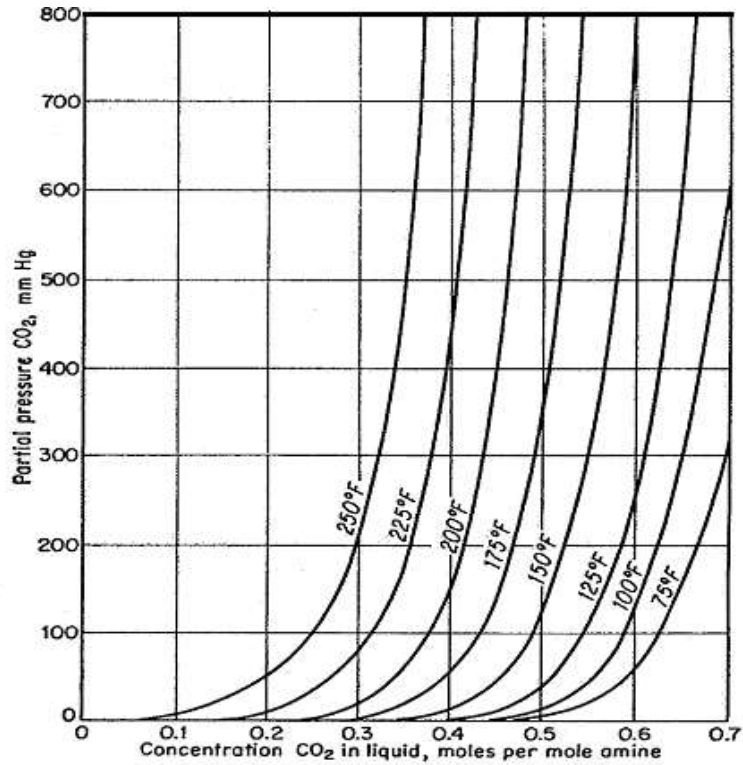


Fig. 16-36. Equilibrium pressure of CO₂ from 15 wt % monoethanolamine solution. (Kohl, 16-45; Mason and Dodge, 16-52. Courtesy AIChE.)

Fig. (5)

The students of the Chemical Engineering Laboratory of the Faculty of Chemistry used the experimental temperature data from the Experimental Data Table (1) and selected the curve at 100 ° F in Fig. (5) to obtain the equilibrium relationship for this experimentation. This requires changing the units of the coordinate axes according to the following diagram in Fig. (6).

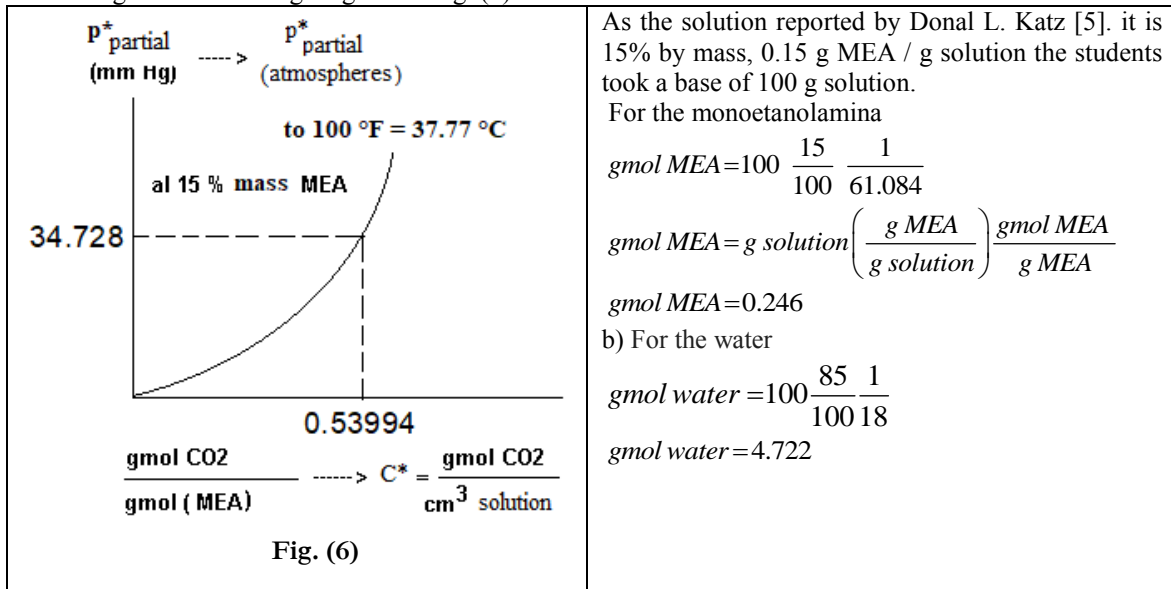
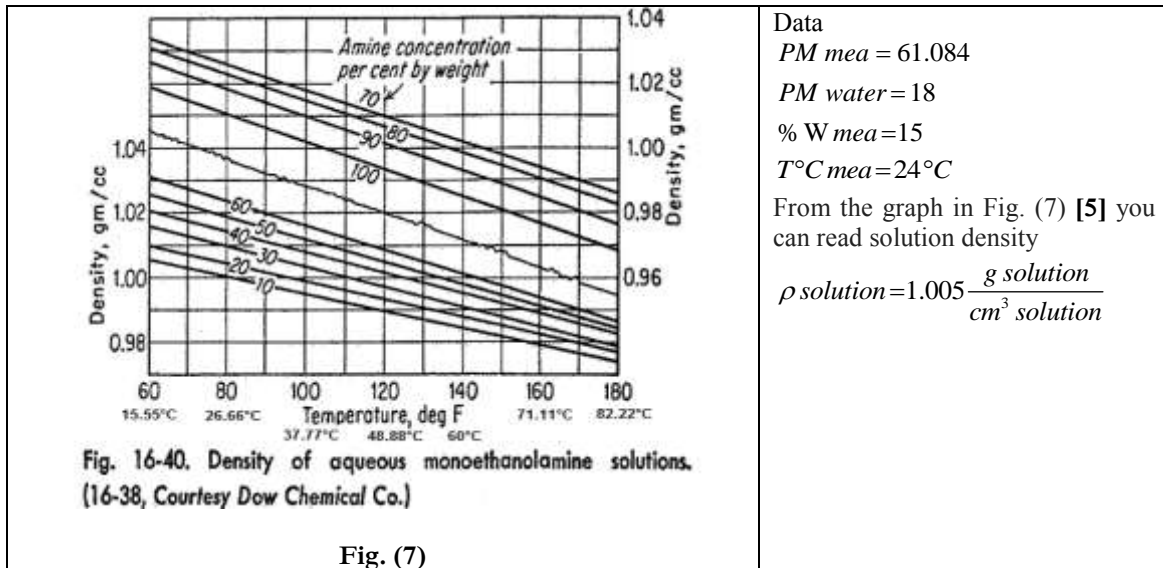


Fig. (6)



Data
 $PM_{mea} = 61.084$
 $PM_{water} = 18$
 $\% W_{mea} = 15$
 $T^{\circ}C_{mea} = 24^{\circ}C$
 From the graph in Fig. (7) [5] you can read solution density
 $\rho_{solution} = 1.005 \frac{g_{solution}}{cm^3_{solution}}$

Fig. (7)

Calculations

$$x_{Molar\ me a} = 0.0494 \frac{gmol\ me a}{gmol\ solution}$$

$$PM_{solution} = x_{Molar\ me a} \times PM_{me a} + (1 - x_{Molar\ me a}) \times PM_{water}$$

$$PM_{solution} = 20.13 \frac{g\ solution}{gmol\ solution}$$

$$\rho_{Molar\ Solution} = \rho_{solution} \times \frac{1}{PM_{solution}}$$

$$\rho_{Molar\ Solution} = 0.05 \frac{gmol\ solution}{cm^3\ solution} = \frac{gmol\ water}{cm^3\ water}$$

Changes in the abscisas

$$0.53994 \frac{gmol\ CO_2}{gmol\ MEA} \frac{0.246\ gmol\ MEA}{4.722\ gmol\ H_2O} \frac{0.5\ gmol\ solution}{cm^3\ solution} = 0.0014 \frac{gmol\ CO_2}{cm^3\ solution}$$

Changes in the ordinates

$$p^*_{atm} = p^*_{mm\ Hg} \frac{1\ atm}{760\ mm\ Hg}$$

Table of Results (1) shows the unit changes for the ordinates and the abscissa

T = 37.77 °C = 100 °F		T = 37.77 °C = 100 °F	
$X^* = \frac{gmol\ CO_2}{gmol\ MEA}$	$p^* = mm\ Hg$	$c^* = \frac{gmol\ CO_2}{cm^3\ solución}$	$p^* = atm$
0	0	0	0
0.05	0	0.00013	0
0.10	0	0.00026	0
0.15	0	0.00039	0
0.20	0	0.00052	0
0.25	0	0.00065	0
0.30	0	0.00078	0
0.35	0	0.00091	0



0.4	0	0.00104	0
0.43908	0	0.00114	0
0.46951	3.2785	0.00122	0.00431
0.49885	9.9449	0.0013	0.01309
0.51433	18.255	0.00134	0.02402
0.525	24.847	0.00137	0.03269
0.53994	34.728	0.0014	0.04569
0.56128	56.058	0.00146	0.07376
0.57409	70.811	0.00149	0.09317
0.58262	85.535	0.00152	0.11255
0.58902	103.50	0.00153	0.13618
0.59756	126.37	0.00155	0.16628
0.60183	142.7	0.00157	0.18776
0.61037	162.31	0.00159	0.21357
0.61677	180.27	0.0016	0.2372
0.62424	200.05	0.00162	0.26322
0.62843	214.74	0.00163	0.28255
0.63261	231.05	0.00165	0.30401
0.63676	253.88	0.00166	0.33405
0.64304	276.72	0.00167	0.36411
0.64934	294.67	0.00169	0.38772
0.65562	317.51	0.00171	0.41778
0.66383	379.47	0.00173	0.4993
0.66587	397.4	0.00173	0.52289
0.67212	425.12	0.00175	0.55937
0.67408	457.72	0.00175	0.60226
0.68032	488.71	0.00177	0.64304
0.68447	509.91	0.00178	0.67093
0.6865	531.1	0.00179	0.69882
0.690	555.56	0.00179	0.731
0.69687	576.54	0.00181	0.75861

B.2 Cálculo de la equilibrium relationships $m \left[\text{atm}/(\text{gmol CO}_2/\text{cm}^3 \text{ sol}) \right]$

$h = 106 \text{ cm}$
 $P_{op} = 0.771 \text{ atm}$
 $P_1 = 0.0643 \text{ atm}$
 $P_2 = 0.023 \text{ atm}$
 $P_{op} \equiv p_{CO_2} \text{ atm}$

Molar fractions were calculated in the tower $y_{top} = 0.02998$ and $y_{bottom} = 0.0834$ using Table (1) of Experimental Data, and were divided into five spaces, with these values the partial p_{CO_2} pressures were calculated

$y_{TopCO_2} = 0.02998$
 $y_{CO_2} = \begin{pmatrix} 0.0298 \\ 0.0405 \\ 0.0512 \\ 0.062 \\ 0.0727 \\ 0.0834 \end{pmatrix}$
 $y_{bottomCO_2} = 0.0834$

$y_{CO_2} \cdot P_{op} \equiv p_{CO_2}$

$p_{CO_2} = \begin{pmatrix} 0.023 \\ 0.0312 \\ 0.0395 \\ 0.0478 \\ 0.0561 \\ 0.0643 \end{pmatrix}$
 $bottom \ p_1 = 0.0643 \text{ atm}$

Top $p_2 = 0.023 \text{ atm}$

Applying Eq. (1)

$$P_{op} = p_1 + \frac{p_2 - p_1}{h} \cdot Z$$

$$Z = \frac{h \cdot (p_{CO_2} - p_1)}{p_2 - p_1}$$

$$Z = \begin{pmatrix} 0 \\ 21.16 \\ 42.321 \\ 63.679 \\ 84.84 \\ 106 \end{pmatrix} \text{ cm}$$

The students of the Chemical Engineering Laboratory found that the potential model adjusts the curvilinear data of the equilibrium

$c^* = \frac{gmolCO_2}{cm^3 \text{ solución}}$	$p^* = atm$
0.00122	0.00431
⋮	⋮
0.00181	0.75861

Top $p_2 = 0.023 \text{ atm}$

$$p_{CO_2} = \begin{pmatrix} 0.023 \\ 0.0312 \\ 0.0395 \\ 0.0478 \\ 0.0561 \\ 0.0643 \end{pmatrix}$$

bottom $p_1 = 0.0643 \text{ atm}$

and found the corresponding concentration values $c^* = (p^*/a)^{1/b}$.

In the potential model they substituted the values of the partial pressures

Finally, the students represented these values as in Fig. (8) with ordinates ($p_{CO_2} = p^*$) vs. abscissa C^* obtaining a practically linear profile from which the equilibrium relations m were calculated for the three experiments as shown in the Results Table (2).

Linear model : $y = m x + b$

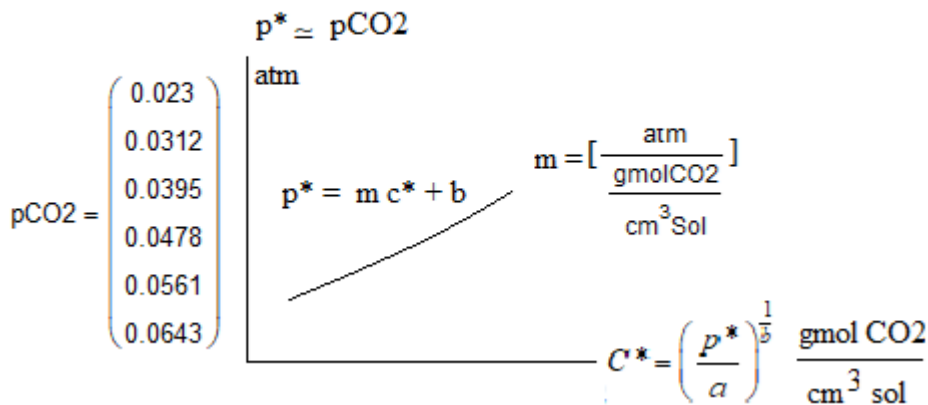


Fig. (8)

Results Table (2)

Flow of feeding (L / h)	Equilibrium relationships m [atm / (gmol CO ₂ / cm ³ sol)]
5	404.141
8	371.312
10	335.176