



# TECHNOLOGY OF TEACHING GRAPHICS OF FREE MECHANICAL VIBRATION USING "MICROSOFT EXCEL" SOFTWARE

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## ANNOTATION

*In this article, harmonic oscillations of a mathematical and spring pendulum are considered, and graphs of the dependence of speed and acceleration on time and coordinates were obtained using the Microsoft Excel software tool.*

**KEY WORDS:** *the equation of motion, velocity, acceleration, amplitude, circular oscillation, the period of oscillation, constant of proportionality, mass, pendulum, spring.*

*Annotatsiya: Ushbu maqolada matematik mayatnik va prujinai mayatniklarning garmonik tebranishi hamda tezlik va tezlanishning vaqtga va koordinataga bog'lanish grafiklari "Microsoft Excel" dasturiy vositasi yordamida yoritilgan.*

*Kalit so'zlar: harakat tenglamasi, tezlik, tezlanishi, amplituda, siklik chastota, tebranish davri, bikrlilik, massa, mayatnik, prujina.*

*Аннотация: В данной статье рассмотрены гармонические колебания математического и пружинного маятника, а также были получены графики зависимости скорости и ускорения от времени и координат, с использованием программного средства "Microsoft Excel".*

*Ключевые слова: уравнение движения, скорость, ускорение, амплитуда, циклическая частота, период колебаний, жесткость, масса, маятник, пружина.*

Informatization of the educational system, the use of modern information technologies and various software tools in the teaching process is one of the urgent issues of today. In particular, in military-academic lyceums and in particular in the "Temurbek maktabi", teaching with the help of computer technologies, showing their graphics using various software tools in the explanation of physical phenomena is an incentive to expand the imagination of the students about the structure of the universe and to form a scientific outlook on objective reality. will be Below we cover the subject of "Harmonic vibrations" which belongs to the "Mechanics" department of physics using the software tool "Microsoft Excel". Usually, in academic lyceums, the topics "Mathematical Pendulum" and "Spring Pendulum" related to the chapter "Mechanical Vibrations and Waves" and the topic of harmonic vibrations are covered extensively. Although the movement of these pendulums is one of the events that happen before our eyes, and all the information about it seems familiar to the readers, there are some aspects that are of special importance. For example, students are familiar with changes of mathematical or spring pendulums only in coordinate axes. However, in this process, not all students are aware of the changes of quantities such as speed and acceleration over time, as well as the laws of connection of these quantities to coordinates. That's why in the article, we will consider in detail all the laws and relationships listed above about information technologies. A mathematical pendulum and also a physical pendulum  $x = A \cos \omega t$  or  $x = A \sin \omega t$  according to the law of harmonic oscillation, we know very well from the science itself. In this  $A$  – vibration amplitude;  $\omega$  – is the cyclic



(circular) frequency of vibration, which is for the mathematical pendulum  $\omega = \sqrt{\frac{g}{\ell}}$  from the formula, and for the spring pendulum  $\omega = \sqrt{\frac{k}{m}}$  is determined using the formula. And the periods of oscillation of these pendulums

$$T = 2\pi\sqrt{\frac{\ell}{g}} \quad \text{va} \quad T = 2\pi\sqrt{\frac{m}{k}}$$

determined using formulas.

If the movement of a ball on a pendulum or a ball attached to a spring starts from the most extreme position from the equilibrium position, then the oscillation is according to the cosine law, that is  $x = A \cos \omega t$  it happens according to the law.

To investigate the time dependence of free harmonic oscillations  $x=x(t)$  we will need to graph the function. We can do this by taking into account the age and psychology of the students, and in order to avoid the complexity of mastering the simplicity of the program, simply by using the Microsoft Excel spreadsheet, which is familiar to all of us. Let's remind, "Microsoft Excel" spreadsheet — there are A, B, C, D, E, ... Columns marked with Latin capital letters such as and 1, 2, 3, 4, ... is an electronic table consisting of lines given by natural numbers such as In this case, each cell comes as an address defined by a column and a row. Each cell contains a number, a word, a logical symbol or a calculation formula. For example, C2 in the cell =2\*4+6 if we write, the result of the calculation will be 14.

Now let's get acquainted with how to create a graph of free harmonic oscillations using this "Microsoft Excel" spreadsheet. This opens an electronic window in which the electronic cells initially have constant values for each pendulum.  $A, g, \ell$  and  $A, m, k$  let's say letters B2, C2, D2 and F2, G2, H2 let's write in the cells. Under the same cells, that is B3, C3, D3 and F3, G3, H3 the values of these quantities corresponding to the cells, let's say 0,05; 9,8; 1 and 0,05; 1; 100 enter numbers. Then, for each pendulum, the cyclic frequency  $\omega$  and the oscillation period T B5, C5 and F5, write in cells G5 and calculate their formulas at the bottom B6, C6 and F6, G6 into the cells (1-picture). As the independent variable of the function, we give different positive values equal to the shares of period T to time t in a separate column, this is starting from cells B9 and F9 downwards. And in the adjacent columns C and G, starting from cells C9 and G9 downwards, the function of the arbitrary variable x, let's say  $x = A \cos \omega t$  function is introduced. Then the corresponding values of voluntary and non-voluntary variables are obtained in adjacent columns. Having marked these columns, the button "Graphic" is selected from the panel window, and from there the option " Pinpoint" is clicked. Then we get the graphs in Figure 1 below. The diagrams in Figure 1 below show how the mathematical and spring pendulums oscillate over time. Since the pictures are exactly similar, we can generalize our idea and say that the graphs in Picture 1 are the vibrational view of all harmonically vibrating bodies. The greater the number of values in one period, the smoother and clearer the graph will be.

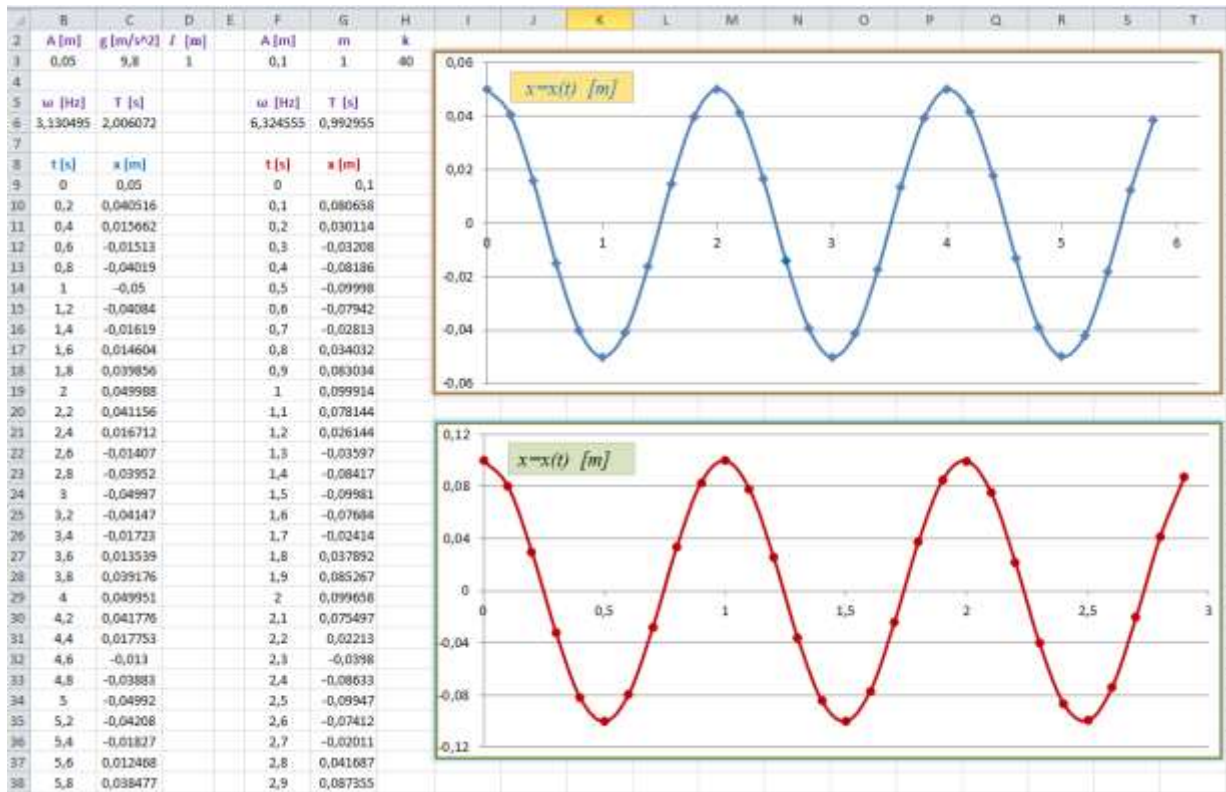


Figure-1

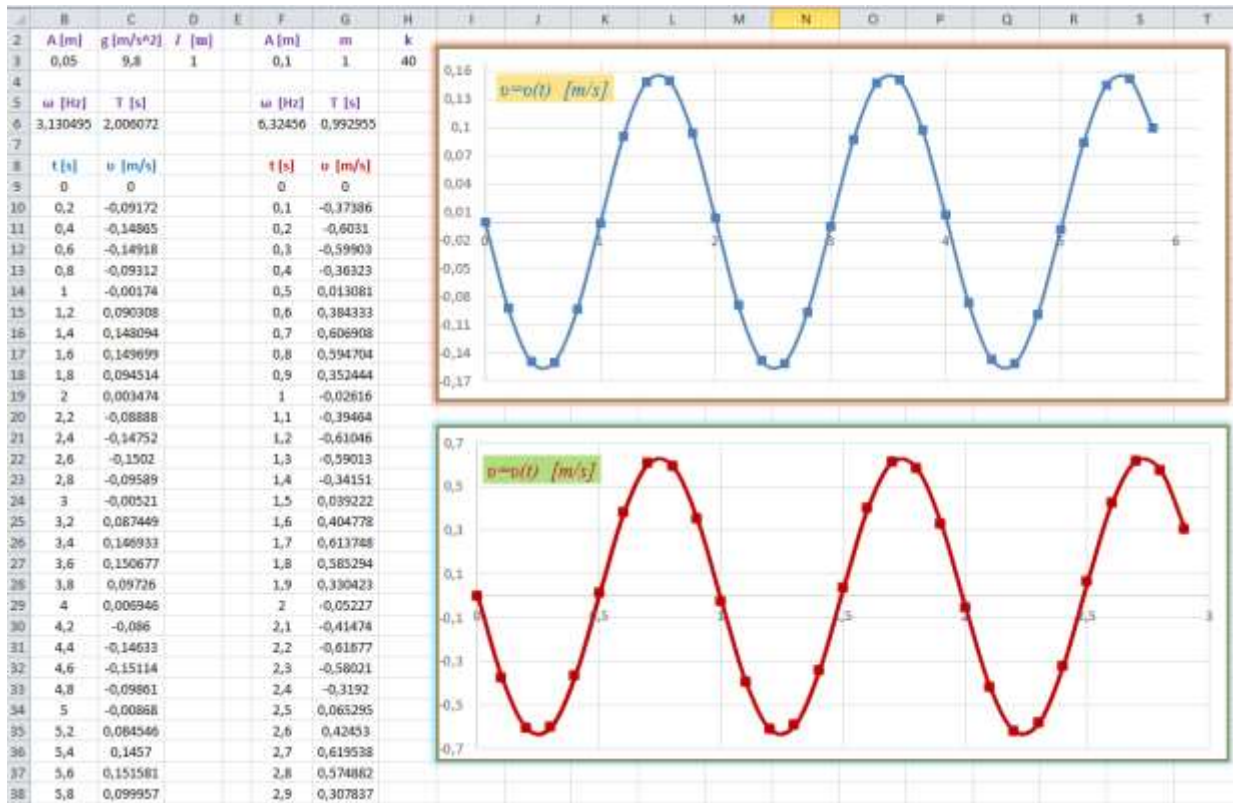
Now let's see how the graphs of speed and acceleration versus time look like.

If the movement of a ball on a pendulum or a ball attached to a spring starts from the most extreme position from the equilibrium position, then the oscillation is according to the cosine law, this is  $x = A \cos \omega t$  it happens according to the law. In this case the velocity functions

$$v = -A\omega \sin \omega t = -A\sqrt{\frac{g}{l}} \sin\left(\sqrt{\frac{g}{l}} t\right) \quad \text{and} \quad v = -A\omega \sin \omega t = -A\sqrt{\frac{k}{m}} \sin\left(\sqrt{\frac{k}{m}} t\right)$$

and acceleration functions  $a = -A\omega^2 \cos \omega t = -\frac{gA}{l} \cos\left(\sqrt{\frac{g}{l}} t\right)$  and  $a = -A\omega^2 \cos \omega t = -A\frac{k}{m} \cos\left(\sqrt{\frac{k}{m}} t\right)$

it will look like. We can generate graphs of these using the Microsoft Excel spreadsheet, just like the equation of motion.



Then we have the graphs in Figure 2 for the velocity equation and in Figure 3 for the acceleration equation.

Figure-2

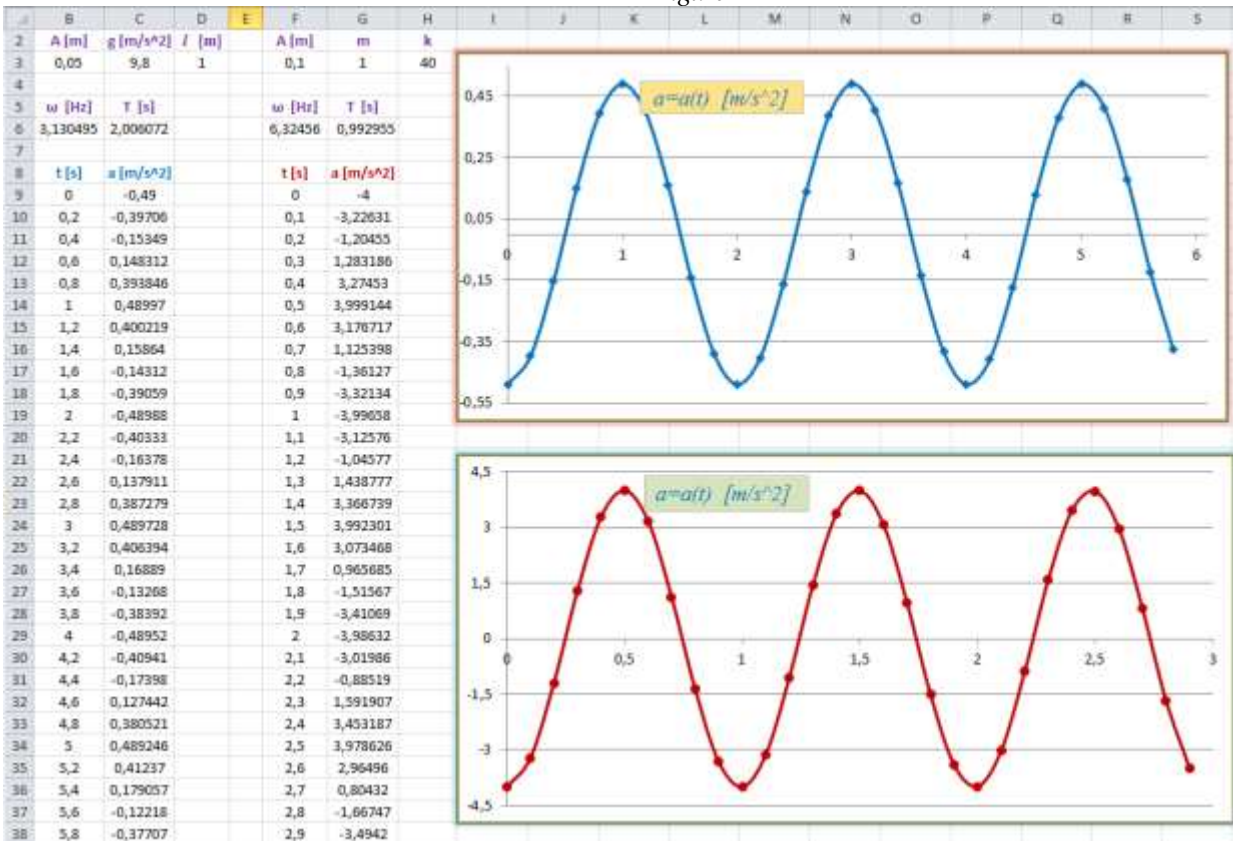


Figure-3



From the figure 1 above and the figures 2 and 3 below, which we have seen, it can be seen that coordinate, velocity and acceleration fluctuations do not occur in exactly one phase. The difference between the oscillation phases of coordinate and velocity and velocity and acceleration is equal to  $\pi/2$ . And the distance between the phases of coordinate and acceleration oscillations differs by  $\pi$ , that is, they oscillate in the opposite phase. In addition, it is necessary to pay special attention to the fact that, regardless of whether it is a mathematical pendulum or a spring pendulum, the equations of motion, speed and acceleration of all harmonically vibrating bodies are similar. Now let's look at how the graphs of the magnitudes of speed and acceleration look like.

To do this, we need to convert the connection of speed and acceleration to time into the form of connection to the coordinate. In this case, we use the trigonometric equation familiar to us from "Trigonometry".

$$\sin^2 \alpha + \cos^2 \alpha = 1, \quad \Rightarrow \quad \begin{cases} \sin \alpha = \pm \sqrt{1 - \cos^2 \alpha} \\ \cos \alpha = \pm \sqrt{1 - \sin^2 \alpha} \end{cases}$$

In addition, the equation of motion of the pendulum  $x = A \cos \omega t$  from  $\cos \omega t = \frac{x}{A}$  we create and use it as well.

$$v = -A\omega \sin \omega t = -A\omega \left( \pm \sqrt{1 - \cos^2 \omega t} \right) = \mp A\omega \sqrt{1 - \left( \frac{x}{A} \right)^2} = \mp \omega \sqrt{A^2 - x^2}$$

$$a = -A\omega^2 \cos \omega t = -A\omega^2 \frac{x}{A} = -\omega^2 x$$

Thus, the connection of the speed of the mathematical pendulum and the spring pendulum to the coordinate

$$v = \mp \omega \sqrt{A^2 - x^2} = \mp \sqrt{\frac{g}{\ell}} (A^2 - x^2) \quad \text{va} \quad v = \mp \omega \sqrt{A^2 - x^2} = \mp \sqrt{\frac{k}{m}} (A^2 - x^2)$$

on the basis of regularity and connection of acceleration to the coordinate  $a = -\omega^2 x = -\frac{g}{\ell} x$  and  $a = -\omega^2 x = -\frac{k}{m} x$

as it changes based on the law. In the velocity equation  $v = \mp \dots$  In the first half of the signs, the (-) sign is selected, and in the second half, the (+) sign is selected.

The connection of velocity and acceleration to the coordinate given above, this is  $v=v(x)$  va  $a=a(x)$  if we make the graphs of the equations using the values given above for myatniks, we will have pictures 4 and 5. In this  $x$  coordinate value  $-A \leq x \leq A$  we have it.



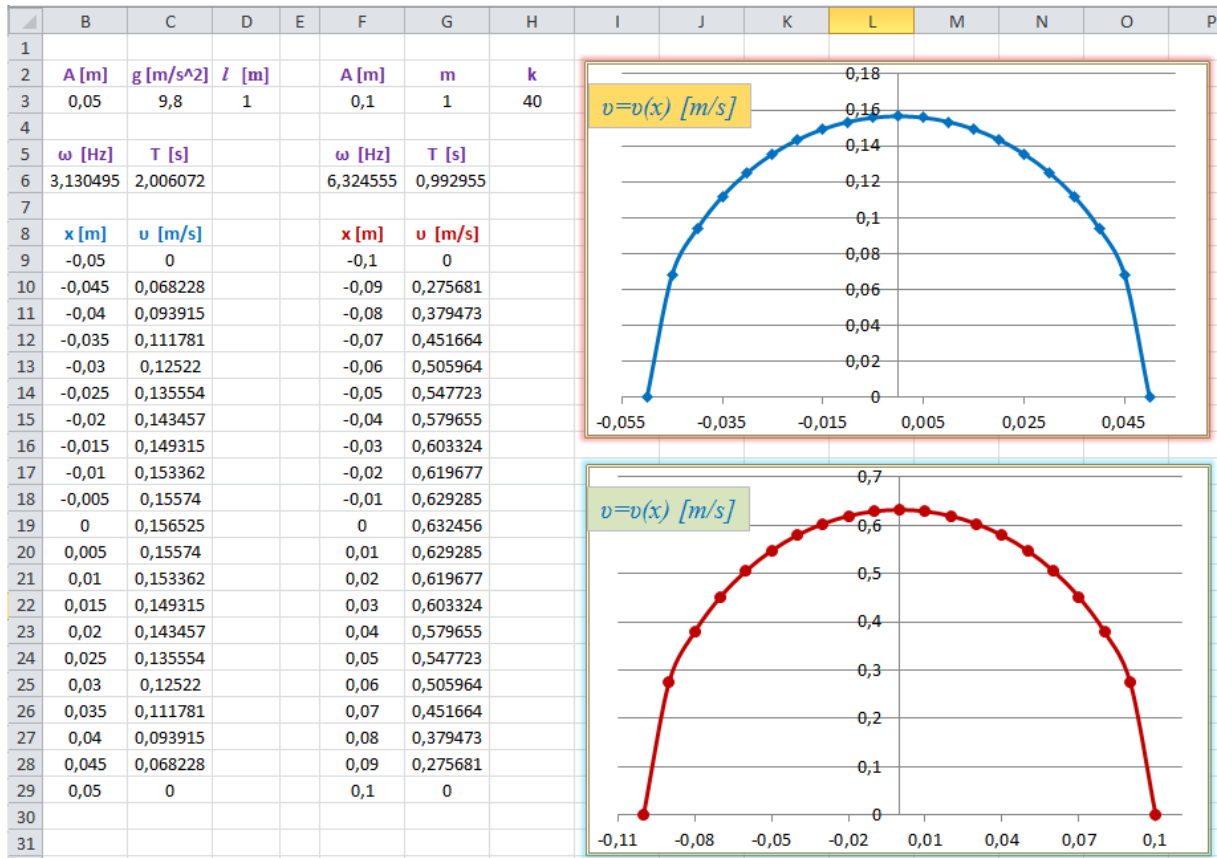


Figure-4

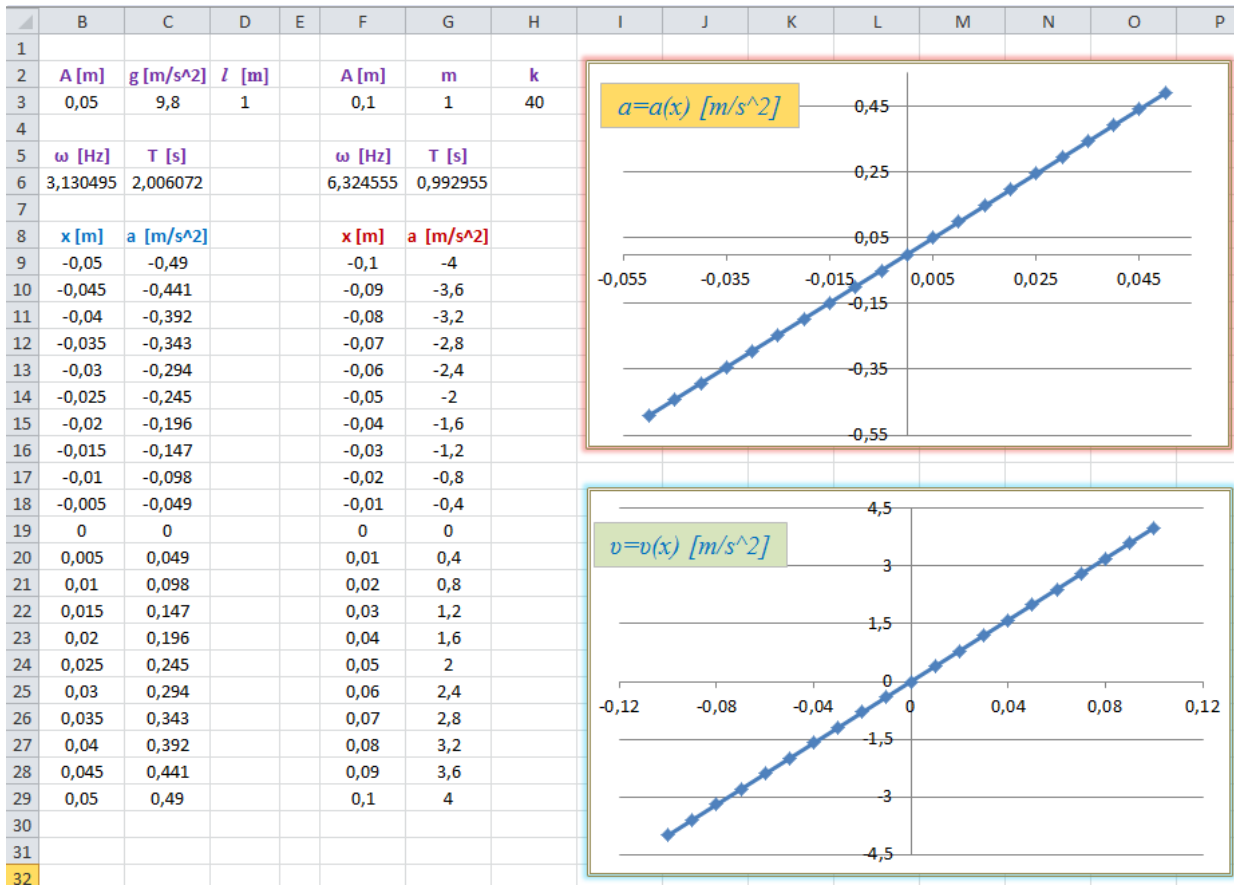


Figure-5

Figures 4 and 5 show that any pendulum (mathematical or spring or other type) with free harmonic oscillation for  $\vartheta=\vartheta(x)$  the graph of the function is in the form of a circular arc,  $a=a(x)$  and the graph of the function is in a linear view.

Thus, we learned how to create graphs of the movement, speed and acceleration of harmonically vibrating bodies using the Microsoft Excel software tool, and we learned that the shape of the graphs does not depend on the type of pendulum. In general, there are many and various software tools that can be used to create these graphs and calculate various quantities in these oscillatory processes. However, from the point of view of the fact that it is easier for students of academic lyceums to understand and master, we chose the software tool "Microsoft Excel".

Advantages of teaching the subject using various modern software tools:

- serves to expand students' thinking and imagination about vibrational processes;
- trains students to use information technologies;
- simplifies calculations and saves time;
- achieved a clear result.

## REFERENCES

1. Akhmedov Sh.B., Dusmuratov M.B. *Physics (Part 2). Textbook for academic lyceum students.* - Tashkent: Navroz, 2020. - 470 p.
2. Ronald J. Hershberger, James J. Reynolds. *Calculus with Applications, the 2nd edition.* Lexington, Mass.: Copyright © 1993 by D.C. Heath and Company.
3. Malikov R.F.. *Workshop on computer modeling of physical phenomena and objects: Proc. allowance.* - Ufa: Publishing House of BashGPU, 2005. - 291p