



HIGH LEVEL COMPARISON - A METHOD OF DETERMINING THE CLASS OF THE DECISION

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ABSTRACT

This article covers complex modules

$$f(x) \equiv 0 \pmod{p_1^{\alpha_1} p_2^{\alpha_2} \dots p_k^{\alpha_k}}$$

comparisons are output to the comparison system, and the solutions of each comparison of the system are determined using the product.

KEYWORDS. Comparison, system of comparisons, product, remainder.

We have a complex module, $f(x) \equiv 0 \pmod{p_1^{\alpha_1} p_2^{\alpha_2} \dots p_k^{\alpha_k}}$ (1) give a comparison.

Here are p_1, p_2, \dots, p_k different prime numbers, $(P_i, P_j) = 1 \quad i \neq j, \quad i = \overline{1, k}, \quad j = \overline{1, k}$.

(1) Comparisons should be required to define a class of solutions. Usually given

(1) is equivalent to the following system of comparison:

$$\begin{cases} f(x) \equiv 0 \pmod{P_1^{\alpha_1}} \\ f(x) \equiv 0 \pmod{P_2^{\alpha_2}} \\ \dots \\ f(x) \equiv 0 \pmod{P_k^{\alpha_k}} \end{cases} \quad (2)$$

(2) the relationship is reasonable that is, comparison of property come turns out to be .[1], [2]

Seconds on the other hand , in general , when a high degree of comparison dice universal formula , solving is not . Therefore, the possibility of boric General without $f(x) \equiv 0 \pmod{P^\alpha}$ (3) solving the training class let's find out. This method is originally $f(x) \equiv 0 \pmod{P}$ (4).

Here $f(x) = a_0x^n + a_1x^{n-1} + \dots + a_n$ (5)

If $n > p$ in (5) , this comparison level $(p-1)$ can be reduced. $f(x) = (x^p - x)Q(x) + R(x)$ (6)



Given the spot $R(x) \equiv 0 \pmod{P^\alpha}$ (5)'in (6) , the comparison in (5) can be written as follows: $(x^p - x) : p$

(5) neither initially module P on the classroom solutions let's learn .

Assumption Let (5) — has a solution and should _ get:

$$x \equiv x_1 \pmod{P} \rightarrow x = x_1 + Pt_1 \quad (7)$$

(7) c (5) ha put her _ decision P^2 module on let's find out

$f(x_1) + Pf'(x_1)t \equiv 0 \pmod{P^2}$ $f(x_1) : P$ Considering

$$\frac{f(x_1)}{P} + f'(x_1)t_1 \equiv 0 \pmod{P} \quad (8)$$

(8) to the decision has _ If $(f'(x_1), P) = 1$ so. $x = x_1 + Pt_1$ with the value of R (x) Taylor in a row distribute P^2 ha caralla hadlar leave will be sent .

The last condition from the solution (8) to the solution has as well as this solution class as follows to obtain :

$$t_1 \equiv t'_1 \pmod{P} \rightarrow x = x_1 + P(t'_1 + P^2t_2) = x_2 + P^2t_2$$

$$x_2 = x_1 + Pt'_1 \quad (9)$$

(9) neither (5) ha put the comparison P^3 module on the solutions class we learn and the yield that was ifodada P^3 can be written as follows: $f(x_2) + f'(x_2)P^2t_2 \equiv 0 \pmod{P^3}$

$\frac{f(x_2)}{P^2} + f'(x_2)t_2 \equiv 0 \pmod{P}$ it's here too ($f'(x_2), P) = 1$ given that the final solution for the comparison above can be written as follow $t_2 \equiv t'_2 + Pt_3$ (10)

(10) neither (9) ha let's put $x = x_2 + P^2(t'_2 + Pt_3) = x_2 + P^2t'_2 + P^3t_3$ Repeating this process $(\alpha - 2)$, the class of general solutions can be written as follows: $x = x_\alpha + P^\alpha t_\alpha$

The above listed method is the following condition reasonable that again while carra emphasizing let's go _ $(f'(x_k, P^k) = 1, \quad k = \overline{1, \alpha}$

The article $f(x) \equiv 0 \pmod{p_1^{\alpha_1} p_2^{\alpha_2} \dots p_k^{\alpha_k}}$ apparently high level comparison to solve the training class comparison to the citation system $f(x) \equiv 0 \pmod{P_i^{\alpha_i}} \quad i = \overline{1, k}$ then discusses the considerations for solving the decision class of each system of comparisons using the product, and the corresponding

$f(x) \equiv 7x^3 + 19x + 25 \equiv 0 \pmod{27}$ comparison decision class
 $x \equiv 13 \pmod{27}; \quad x = 13 + 27t_3$ found.

For example . $f(x) \equiv 0 \pmod{3^3}$ (11) $f(x) = 7x^3 + 19x + 25$



$$f(x) \equiv 7x^3 + 19x + 25 \equiv x^3 + x + 1 \equiv 0(\text{mod}3), (x^3 - x) + 2x + 1 \equiv 0(\text{mod}3)$$

$$(x^3 - x) : 3 \rightarrow 2x \equiv -1(\text{mod}3), 2x \equiv 2(\text{mod}3), x \equiv 1(\text{mod}3) \quad x = 1 + 3t_1 \quad (12)$$

(12) to (11) release $_3^2$ Ha divisible limits leave send

$$f'(x_1) = (28x^3 + 19)x \equiv 47, \quad f(1) = 51, f(1) + f'(1)3t_1 \equiv 0(\text{mod}3^2),$$

$$51 + 3 \cdot 47t_1 \equiv 0(\text{mod}3^2), 17 + 47t_1 \equiv 0(\text{mod}3), \quad -2 + 2t_1 \equiv 0(\text{mod}3),$$

$$t_1 \equiv 1(\text{mod}3), t_1 = 1 + 3t_2 \quad (13)$$

(13) to (12) let's put $x = 1 + 3(1 + 3t_2) = 4 + 3^2t_2 \quad (14) \quad x_2 = 4$

$$f(4) = 7 \cdot 4^3 + 19 \cdot 4 + 25 = 7 \cdot 64 + 76 + 25 = 549$$

$$f'(x) = 21x^2 + 19, f'(4) = 21 \cdot 4 + 19 = 84 + 19 = 103, 549 + 103 \cdot 3^2t_2 \equiv 0(\text{mod}27)$$

$$61 + 103t_2 \equiv 0(\text{mod}3), \quad 1 + t_2 \equiv 0(\text{mod}3), t_2 \equiv 2 + 3t_3 \quad (15)$$

(15) to (14) put the last $_x = 4 + 3^2(2 + 3t_3) = 13 + 3^3t_3$.

USED LITERATURE

1. Vinogradov I. M. "Fundamentals of the theory of the bit" Nauka Moscow, 1974.
2. Soliev A., Isroilov M. "Sonlar theory" T.: 1993.
3. Nazarov R.N., Toshpulatov B.T. "Algebra and number theory" T.: 1993.
4. Sh.A. Ayupov, B.A. Omirov "Algebra and number theory" T.: 2019.
5. J. Khodjiev, A.S. Fineleib "Algebra and number theory courses" T.: 2001.